Image Analysis

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Overview

- Digital image
- 2. Image Analysis
- 3. Point Operations
- 4. Local Filtering
- 5. Filtering in the frequency domain
- 6. Image Restoration
- 7. Segmentation

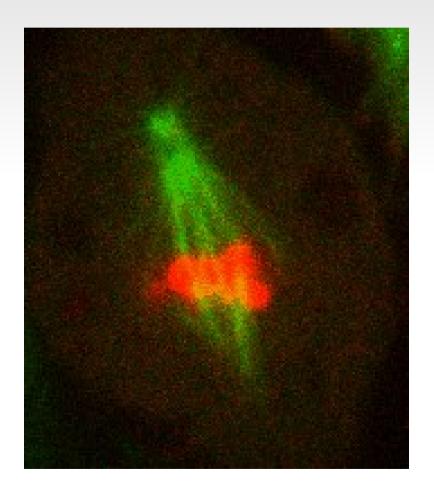
- 8. Geometrical Transformations
- 9. Visualization
- 10. Colocalization
- 11. Filament Tracing
- 12. Particle Tracking
- 13. Cell Tracking
- 14. Software Tools

What is a digital image - examples

Example 1: Fly Brain example (ImageJ)



Example 2: Mitosis (ImageJ)



Example 3: Embryonic Zebrafish Heart Development

What is a digital image - mathematical point of view

- Matrix of sample values
 - finite number of samples
 - finite number of values per sample

- Image dimensions
 - 1D, 2D, 2D + t, 3D, 3D + t, 3D + t + multispectral
 - $I_{(x,y,z,t)} \in W^n$

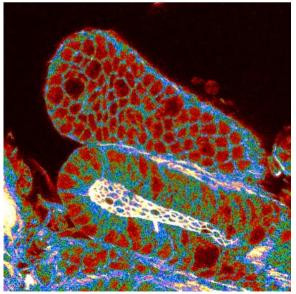
```
10
                                 12
                                      13
                                          14
                                               11
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              7
                            25
                                                    16
                       17
                                 30
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                                          29
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                                          53
                                               41
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         19
             29
                   44
                            72
                                               61
                                                    45
                       60
                                      73
                                                             19
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                                 102 98
                                                    59
                                                                  13
    14
                   61
                       79
                            94
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                                                         43
                                                             26
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              56
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12
    23
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              62
                   87
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12
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                                                                       13
                                                                  21
    21
         37
              54
                                          88
                                               80
                                                    67
                                                         56
                                                             41
                   80
                       102 108 103 96
                                          80
    17
         28
              44
                   62
                       75
                            84
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                                          18
                                               16
                                               3
```

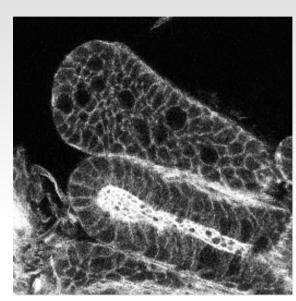
What is a digital image - displayed by the computer

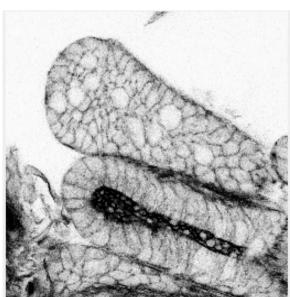
- mapping between sample values and display colors
 - bright means high values
 - bright means low values
 - brightness / contrast adjustments
 - lookup tables

When I use a word," Humpty Dumpty said, in rather a scornful tone, "it means just what I choose it to mean—neither more nor less.

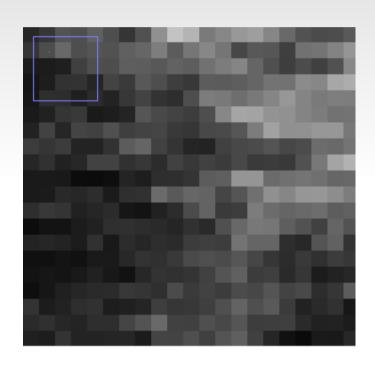
L. Carroll, Through the Looking-Glass



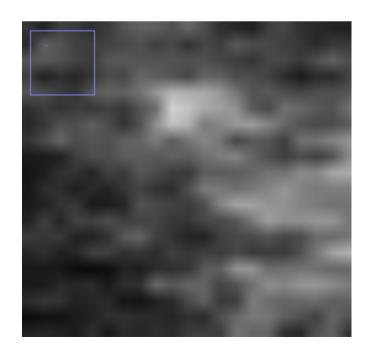




What is a digital image - displayed by the computer



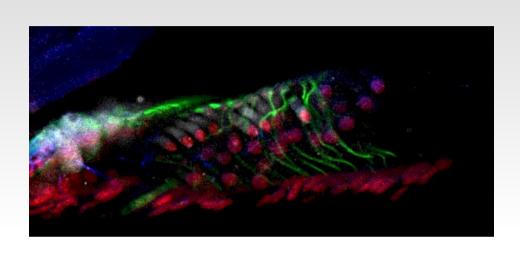
- mapping between sample grid and display grid
 - homogenous rectangles
 - interpolation

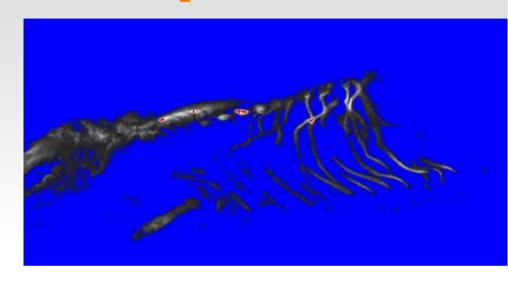


What is a digital image - represented in memory

Formats	Values	Interpretation
8-bit	0-255	unsigned integer
16-bit	0-65535	unsigned integer
32-bit	-3.4×10 ³⁸ - +3.4×10 ³⁸	precision 6-7 decimal digits, special values like NaN for "Not a Number", Infinity and -Infinity
8-bit + lookup table	0-255	indexed color
24-bit	3 times 0-255	RGB
hyperstack	n channels of 8, 16 or 32 bit	3d + time + n channels

What is a digital image - convertion traps





- look at green channel
- multiply by ten
- convert both to 8-bit
- compare total intensity before and after

Label	Mean	Min	Max	IntDen
green	100.9	0	4095	13774198
10 x green	1009.0	0	40950	137741980
green 8bit	6.3	0	255	861340
10 x 8bit	6.3	0	255	861340

 conversion is done by linearly scaling from min–max to 0–255

What is a digital image - stored on a disk

- data (sample values) + meta-data in header
- different organization of data and meta-data
- different possibilities / restraints

format	name	provider	properties
tiff	Tagged image file format	Adobe	lossless / metadata
ome-tiff	Open microscopy environment-tiff	OME	tiff with ontology for microscopy metadata
jpeg exif	Joint Photographic Experts Group - exchangable image file format	ISO	lossy data compression / minimal metadata
lsm, stk	Laser scanning microscope file	Zeiss	extensions of tiff
lif	Leica image file format	Leica	can contain multiple images in one file

What is a digital Image - stored on a disk

some lsm-metadata

BitsPerPixel 8

DimensionOrder XYCZT

IsInterleaved false

IsRGB false

LittleEndian true

PixelType uint8

Series 0 Name cafe

SizeC 2

SizeT 1

SizeX 1320

SizeY 1320

SizeZ 1

BeamSplitter #1 Acquire true

BeamSplitter #1 Filter None

BeamSplitter #1 Filter Set FW1

BeamSplitter #1 Name FW1

DC#1 Pinhole Diameter 896.0

DC#1 Pinhole Name PH1

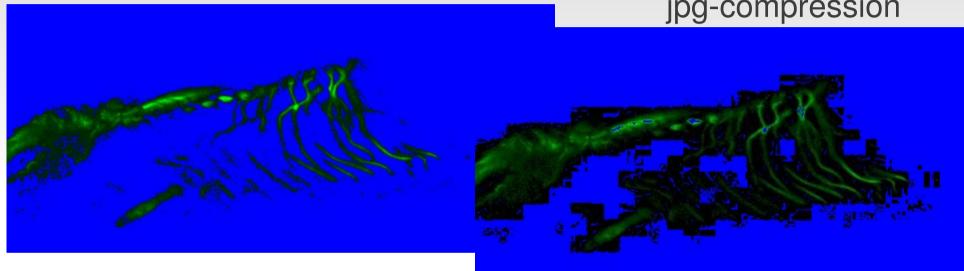
DC#1 SPI Wavelength End 798.88

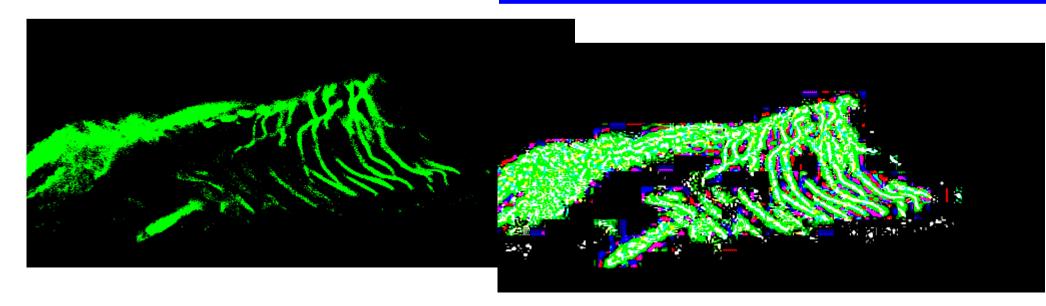
DC#1 SPI Wavelength Start 456.48

. . .

What is a digital Image - stored on a disk

artefacts from jpg-compression

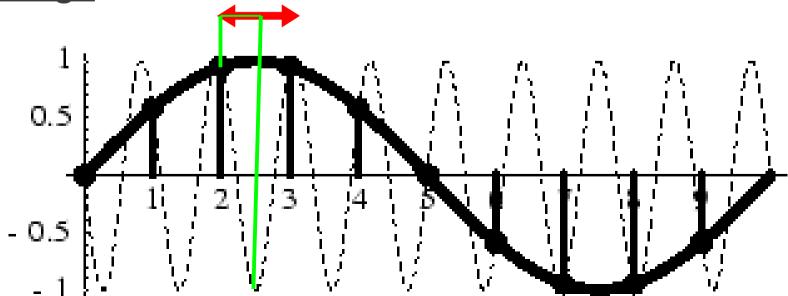




What is a digital image - the image and the real world

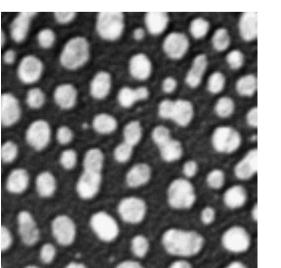
- sampling and resolution
- digital image finite number of samples
- Nyquist-Shannon sampling theorem:

The sampling interval must be smaller than one-half the size of the smallest resolvable feature of the optical image



What is a digital image - the image and the real world

- sampling and resolution
- resolution of an optical system
 - the smallest distance at which two objects can still be distinguished
 - given by the Rayleigh criterion $r = \frac{0.61 * \lambda}{NA}$
- therefore the pixel size must be

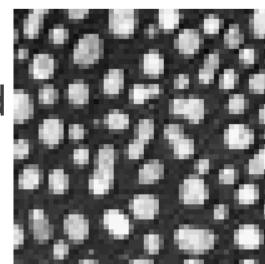


$$\Delta x < \frac{\lambda_{em}}{4 * NA}$$

$$\Delta x < \frac{\lambda_{ex}}{2}$$

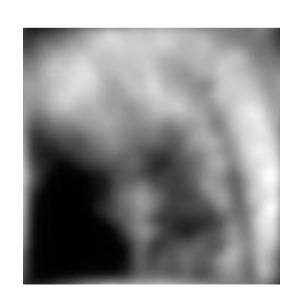
for widefield

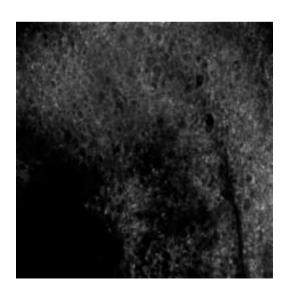
for confocal

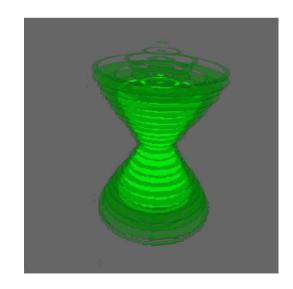


What is a digital image - the image and the real world

- point spread function
 - the way an optical system images one point
 - a point = an object at the limit of the resolution
 - acquired image = object function convolved with psf

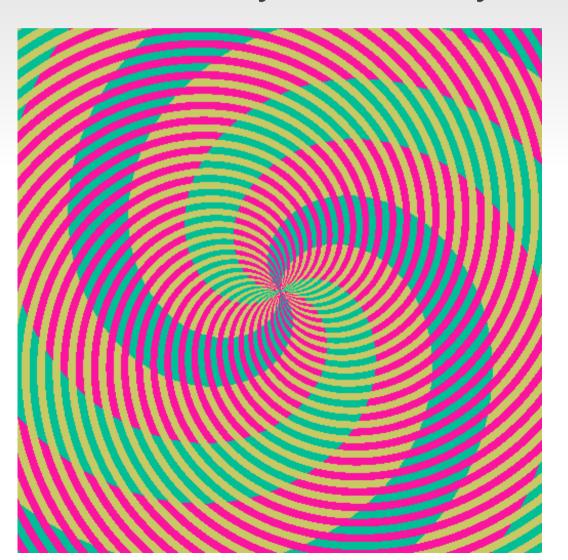




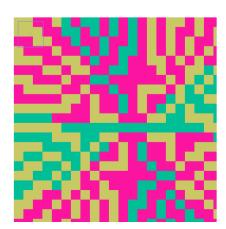


What is a digital image - image and perception

How many colors do you see?

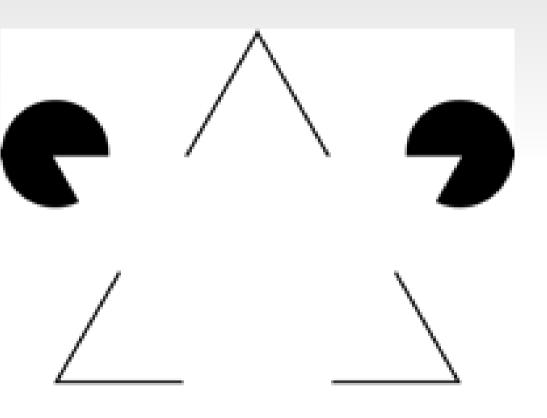


- the image contains3 different colors
- the brain interprets color according to the background



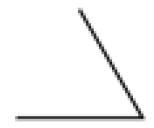
What is a digital image - image and perception

Can you see the white triangle, standing on its head?



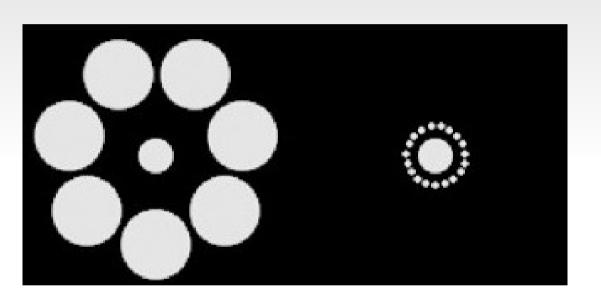
- the borders of the triangle don't exist
- the brain connects
 the points and
 interprets the scene
 as one triangle on
 top of another one





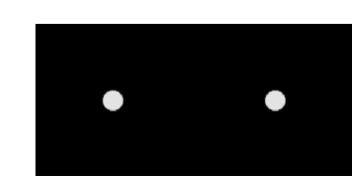
What is a digital image - image and perception

Which of the two central spots is bigger?



- both have the same size
- again the interpretation is relative to the environment

- conclusions
 - we can not always trust our senses when comparing images
 - quantification needed

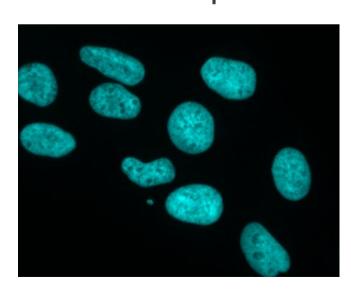


What is image analysis?

Wikipedia

 "Image analysis is the extraction of meaningful information from images; mainly from digital images by means of digital image processing

techniques."

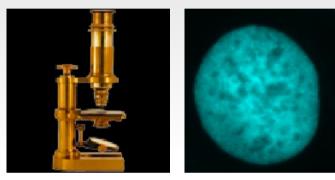


	Area	Perim.
1	6101	353.061
2	7047	329.120
3	5455	292.392
4	7524	328.191
5	5653	300.978
6	6178	304.392
7	4583	296.392
8	7312	333.120
9	6820	343.345

IMAGE IN – FEATURES OUT

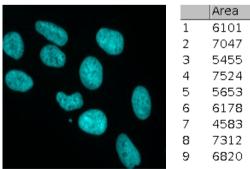
Image analysis and related concepts

image acquisition



object in → image out

image analysis



	Area	Perim.	
1	6101	353.061	
2	7047	329.120	
3	5455	292.392	
4	7524	328.191	
5	5653	300.978	
6	6178	304.392	
7	4583	296.392	
8	7312	333.120	
9	6820	343.345	

image in — features out

image processing

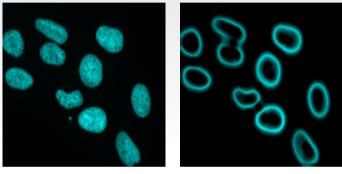
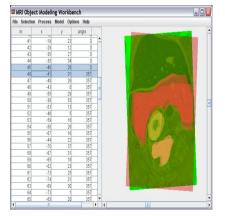


image in → image out

visualization



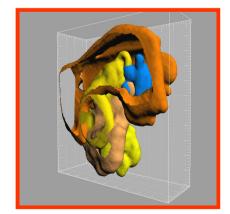
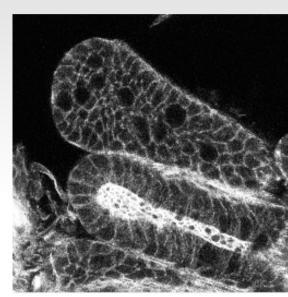
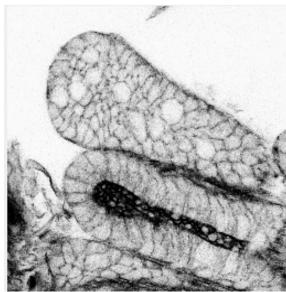


image in → representation out

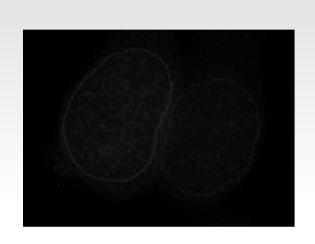
Point operations

- global intensity transformations
 - intensity inversion
 - contrast and brightness adjustment
 - linear
 - gamma function
 - histogram equalization
 - pseudo-coloring
 - intensity thresholding

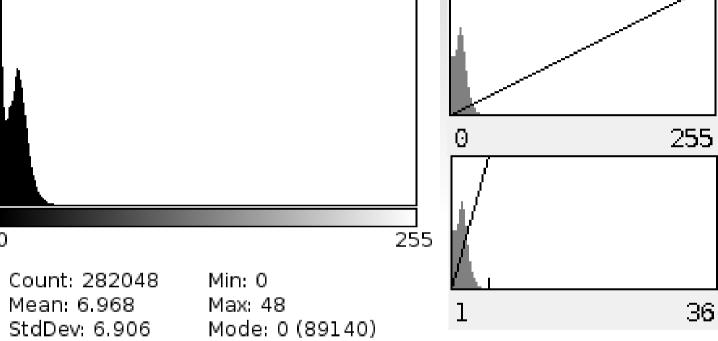


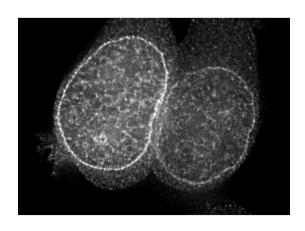


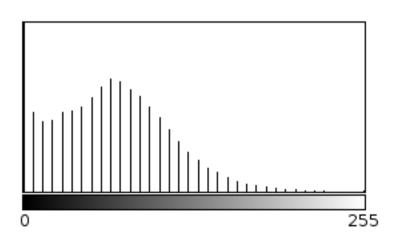
Point operations contrast stretching





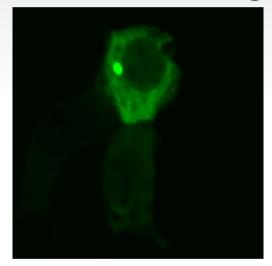


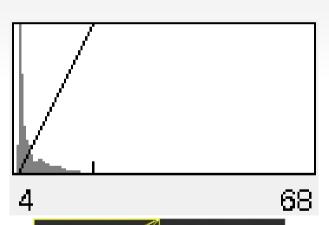


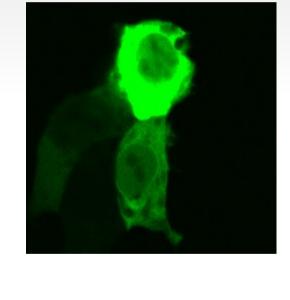


Point operations - gamma function

- linear function
 - changes small and high values in the same way

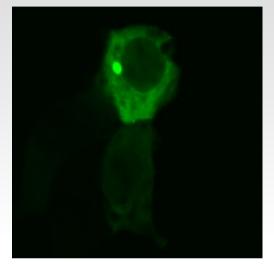


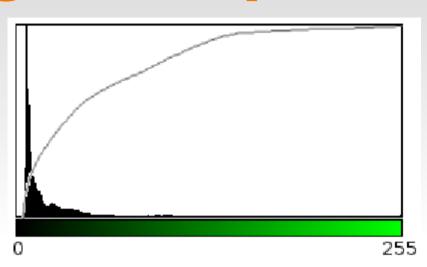


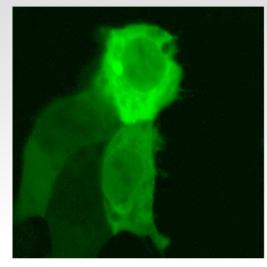


$$f(i) = \left(\frac{i}{255}\right)^{\frac{1}{\gamma}} \cdot 255$$

Point operations - histogram equalization

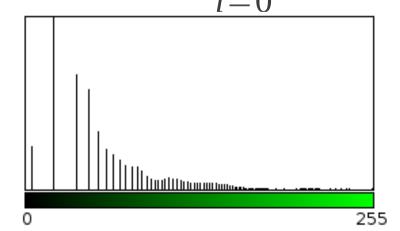




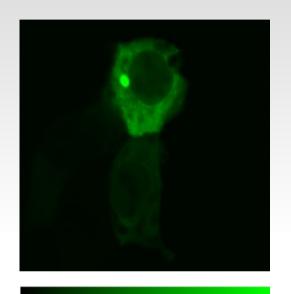


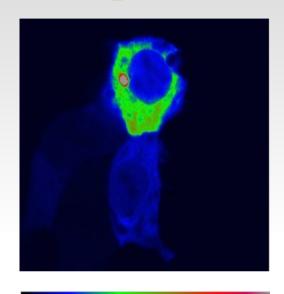
- calculate cumulative histogram
- normalize to range 0-255

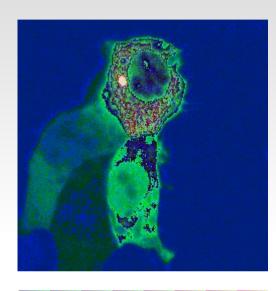
$$h'(n) = \sum_{i=0}^{\infty} h(i)$$



Point operations - lookup tables

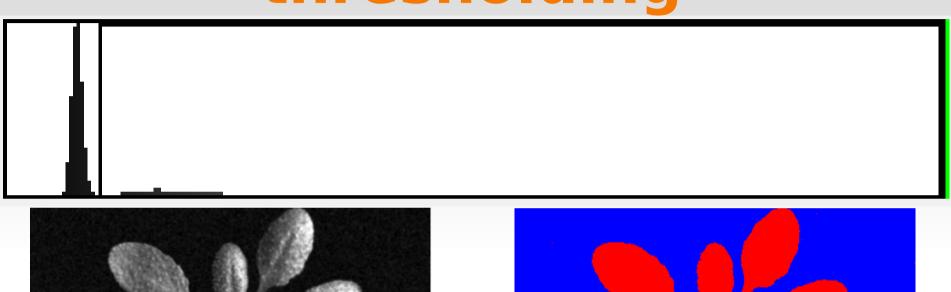


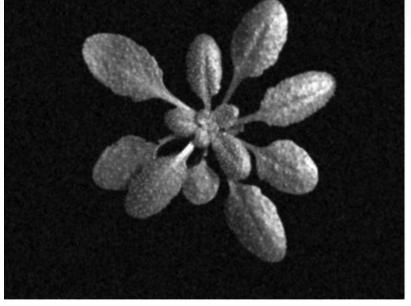


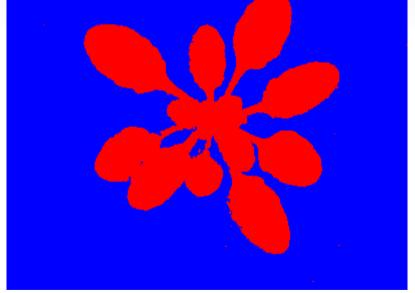


Index	Red	Green	Blue
0	0	0	0
1	0	0	5
2	0	0	10
3	0	1	15
4	0	1	20
5	0	1	25

Point operations - thresholding







- segmentation separate objects from background what threshold value?
- can be done by applying a global threshold

the same for all images?

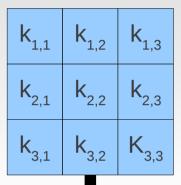
Local Filtering

- convolution filter (linear filtering)
 - smoothing
 - mean filter
 - gaussian blur filter
 - edge detection
 - sobel filter
 - spot detection
 - Laplacian of Gaussian (Mexican Hat Filter)
- ranking filter
 - median, min, max
- mathematical morphology
 - post processing
 - erode, dilate, open, close, top hat, granulometry

The new value of a pixel is calculated from the values in the local neighborhood of the pixel

Local Filtering convolution filter

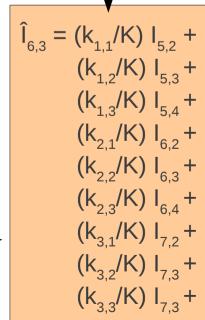
kernel



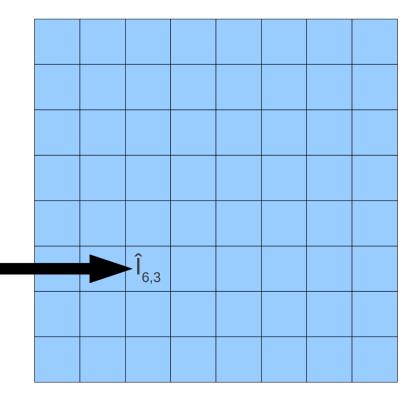
$$K = k_{1,1} + ... + k_{3,3}$$

input image

I _{1,1}					I _{1,8}	
I _{2,1}						
	I _{5,2}	I _{5,3}	I _{5,4}			
	I _{6,2}	l _{6,3}	I _{6,4}			
	l _{7,2}	I _{7,3}	I _{7,4}			



result image



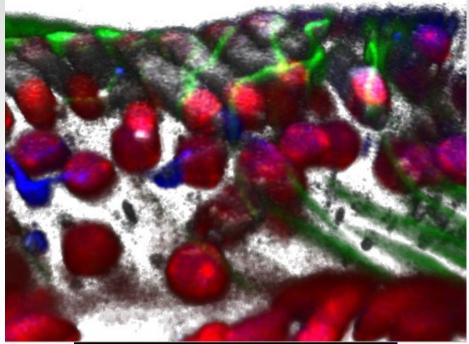
mean

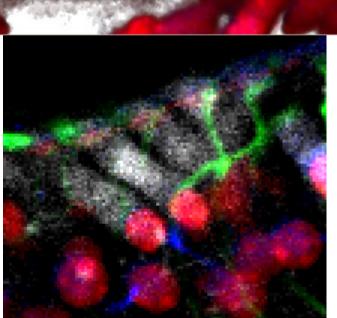
Convolution filter - smoothing

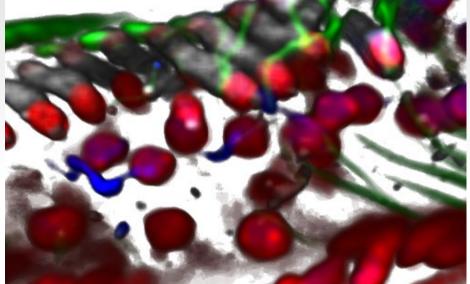
 1
 1

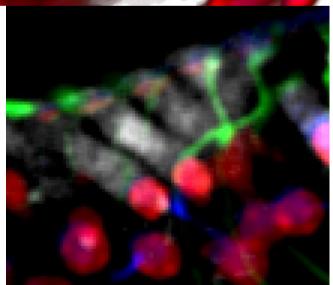
 1
 1

1 | 1 | 1

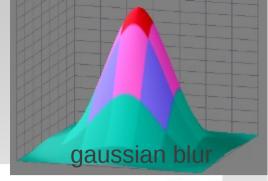


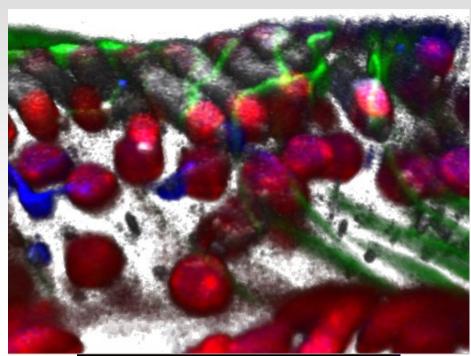


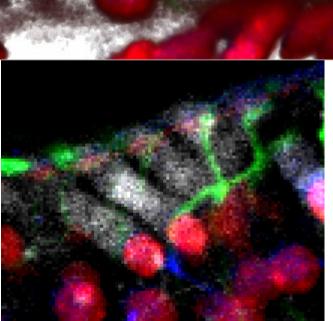


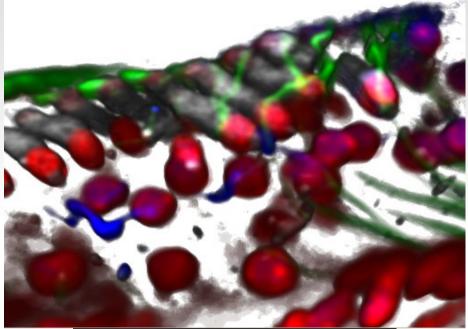


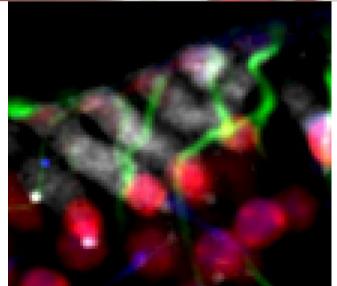
Convolution filter smoothing







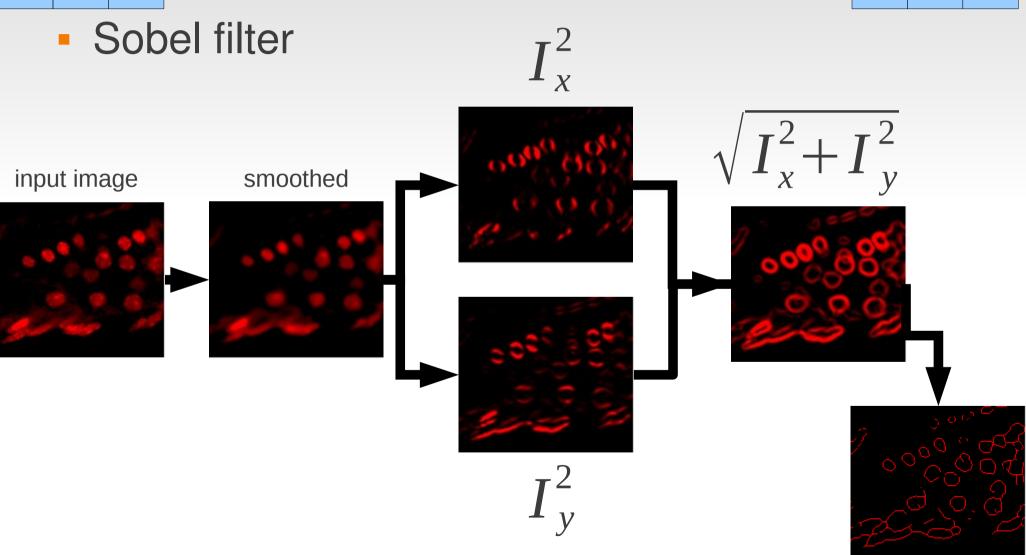




1 0 -1 2 0 -2 1 0 -1

Convolution filter - edge detection

1	2	1
0	0	0
-1	-2	-1

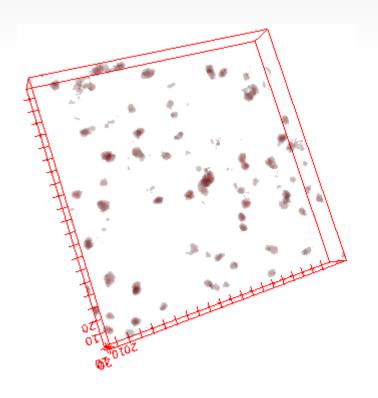


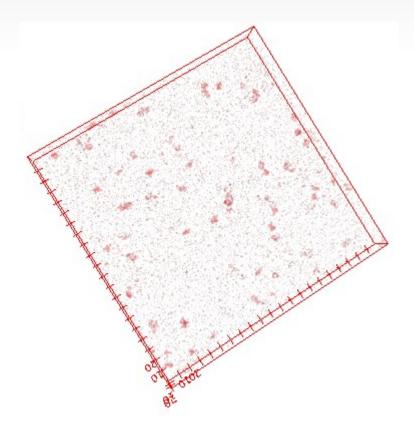
laplacian

Convolution filter - spot detection

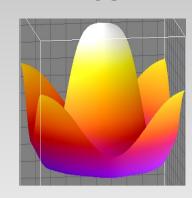
-1	-1	-1
-1	8	-1
-1	-1	-1

- Laplacian filter enhaces spots but augments noise
- use 'Laplacian of Gaussian (LoG)' to enhance spots in noisy images

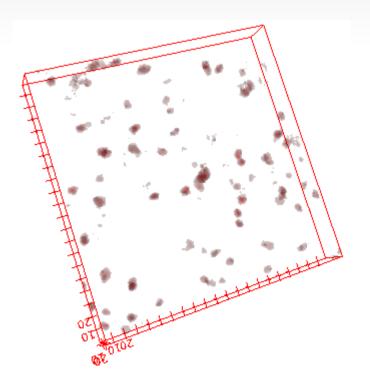


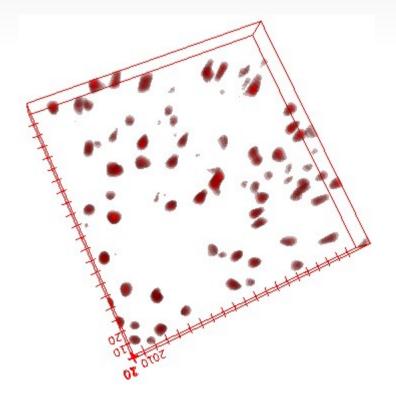


Convolution filter - spot detection



- Laplacian filter enhaces spots but augments noise
- use 'Laplacian of Gaussian (LoG)' to enhance spots in noisy images





Local Filtering - Ranking filter

- for each pixel:
 - sort the values in the neighborhood
 - take the value at a given position

first = min filter

enlarge dark regions

middle = median filter

filter noise

last = max filter

enlarge bright regions

15	18	14	
29	27	13	
12	19	21	

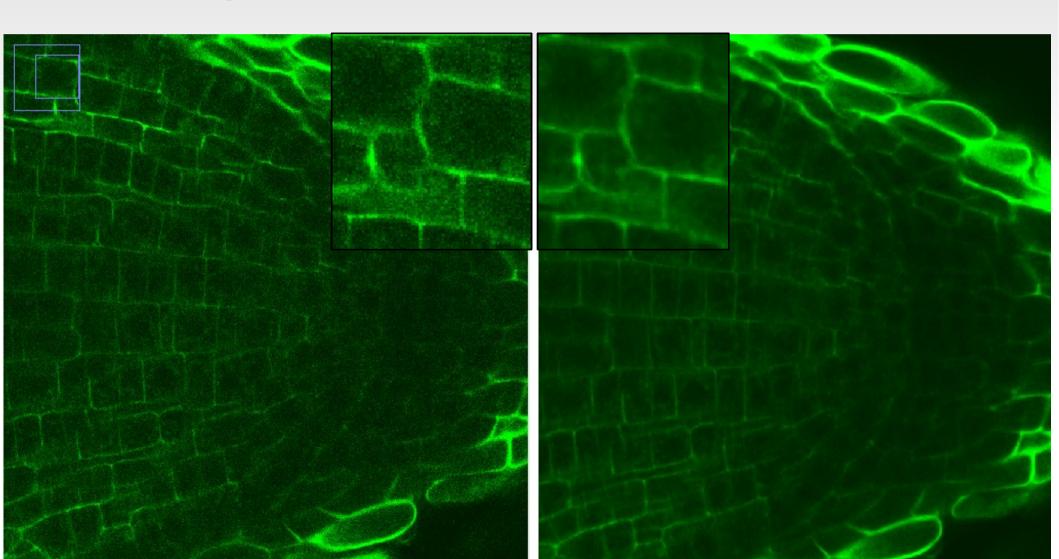
15	18	14
29	18	13
12	19	21

12, 13, 14, 15, **18**, 19, 21, 27, **29**

Ranking filter - median filter

+ stable against outliers

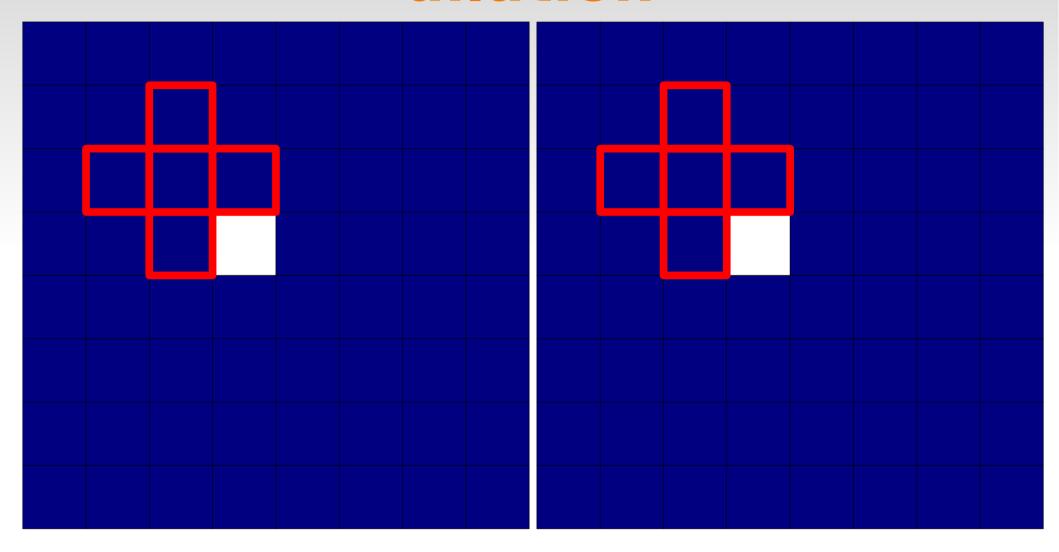
- can be long to calculate

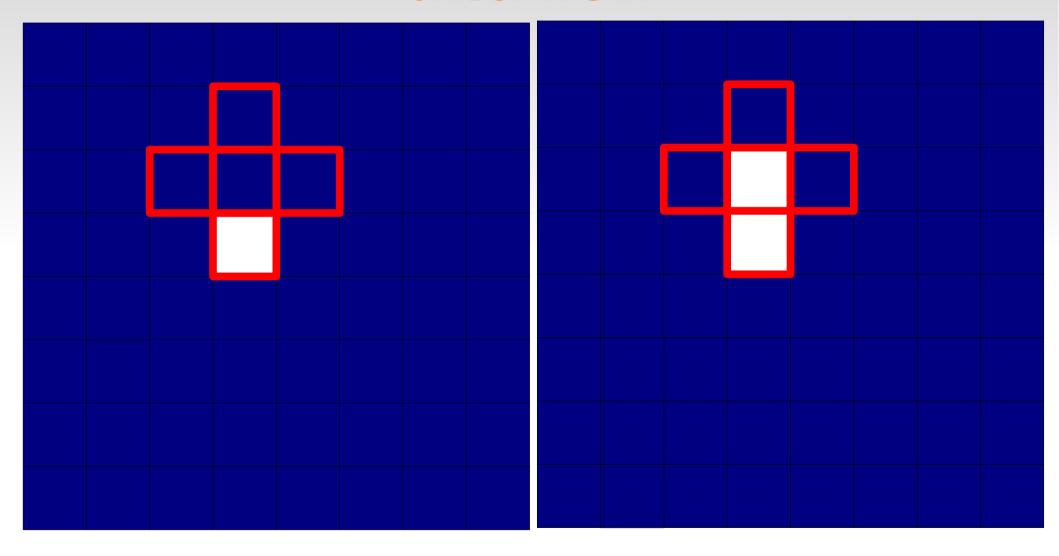


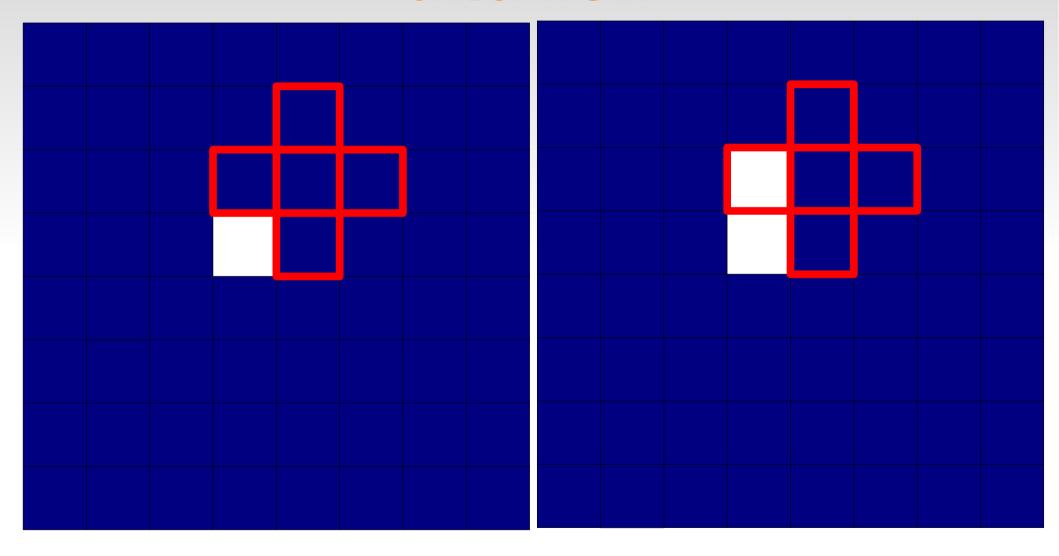
Local Filtering binary morphology

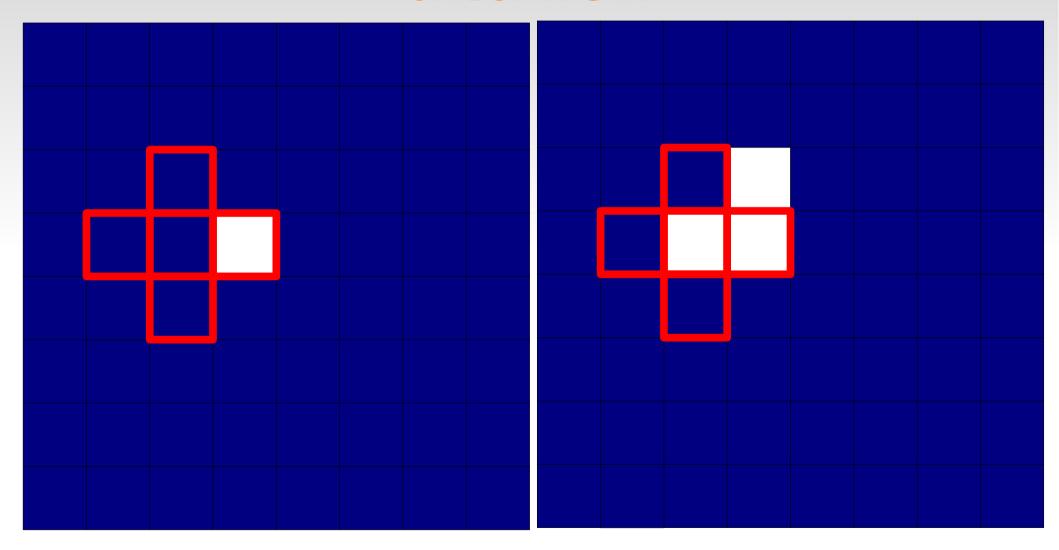
- correct segmentation, measure features, granulometry, edge detection, skeletonization, reconstruct objects
- work on a mask (a binary image)
- move the structuring element along the image
- two basic operations
 - dilate (enlarge objects):
 - current pixel is 1 if the SE touches a 1 in the image
 - erode (shrink objects):
 - current pixel is 1 if no 1 in the SE touches a zero in the image

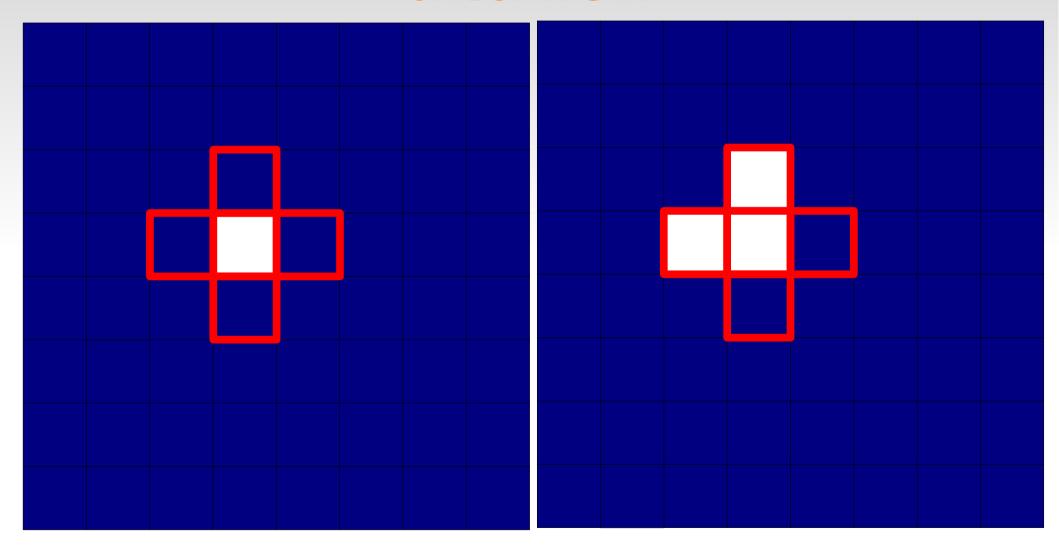
Binary Morphology - dilation

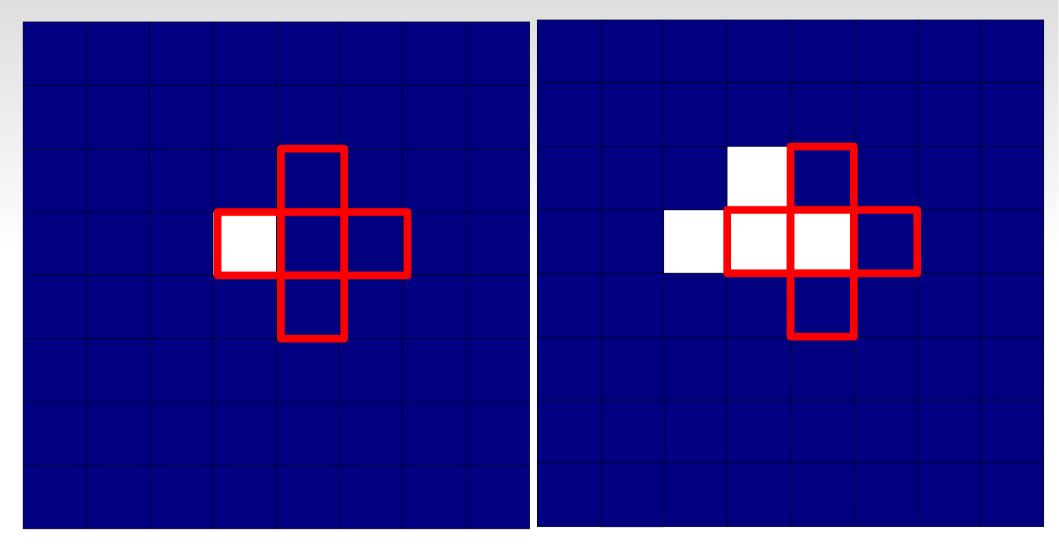


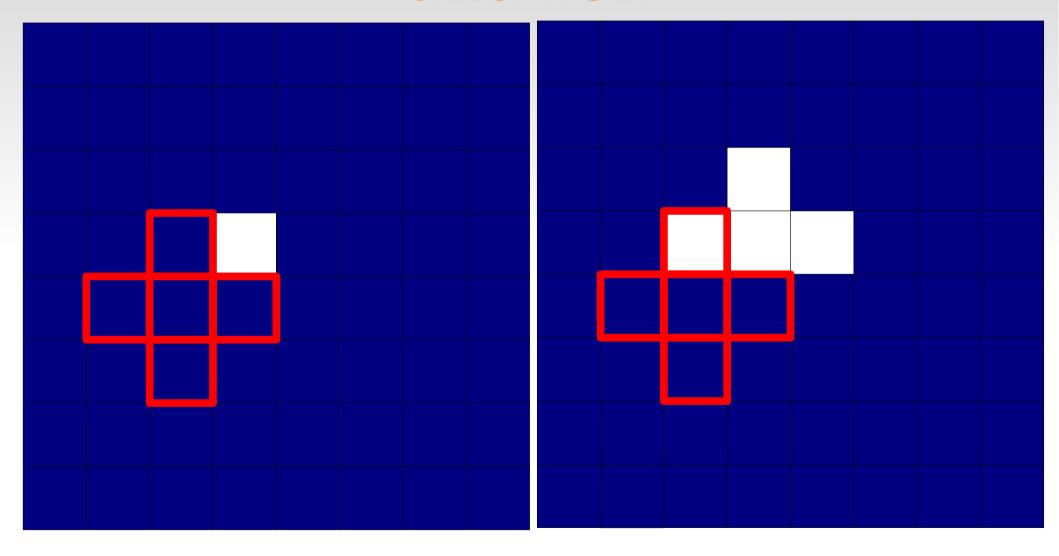


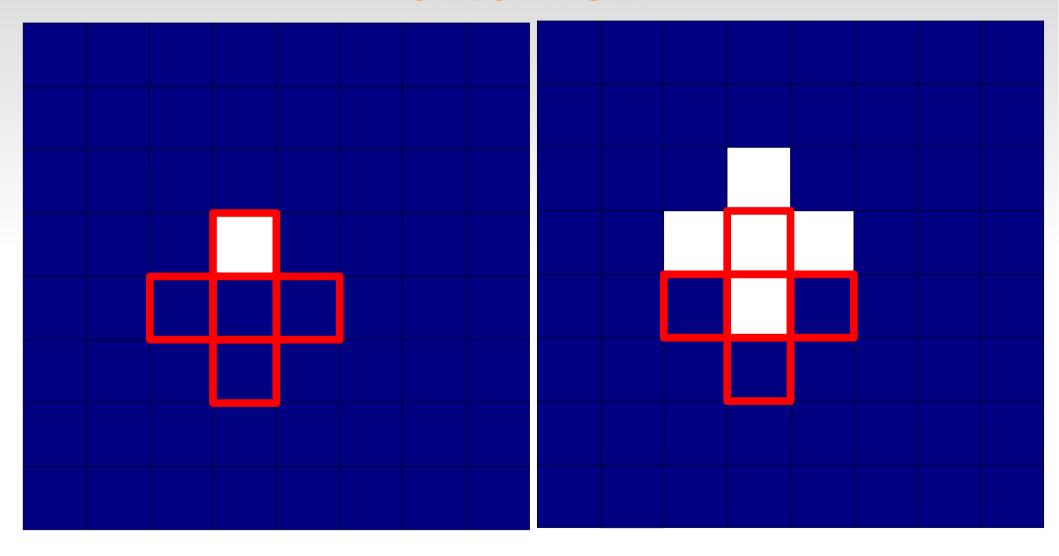


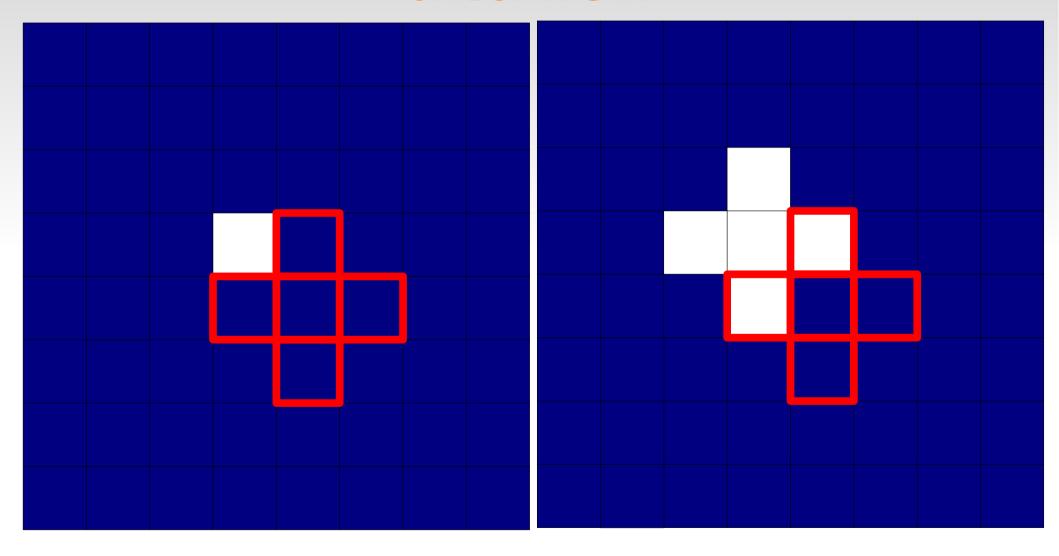


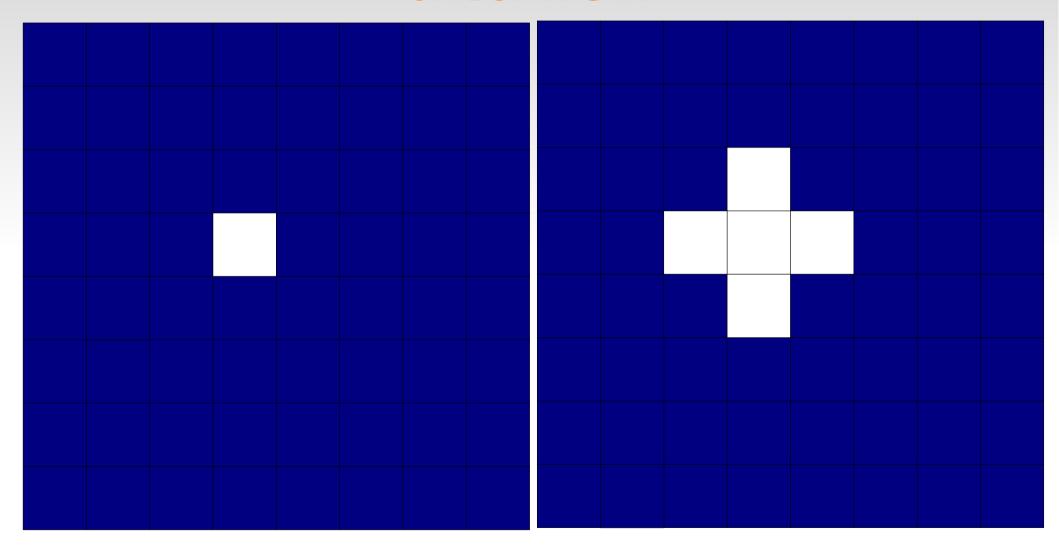


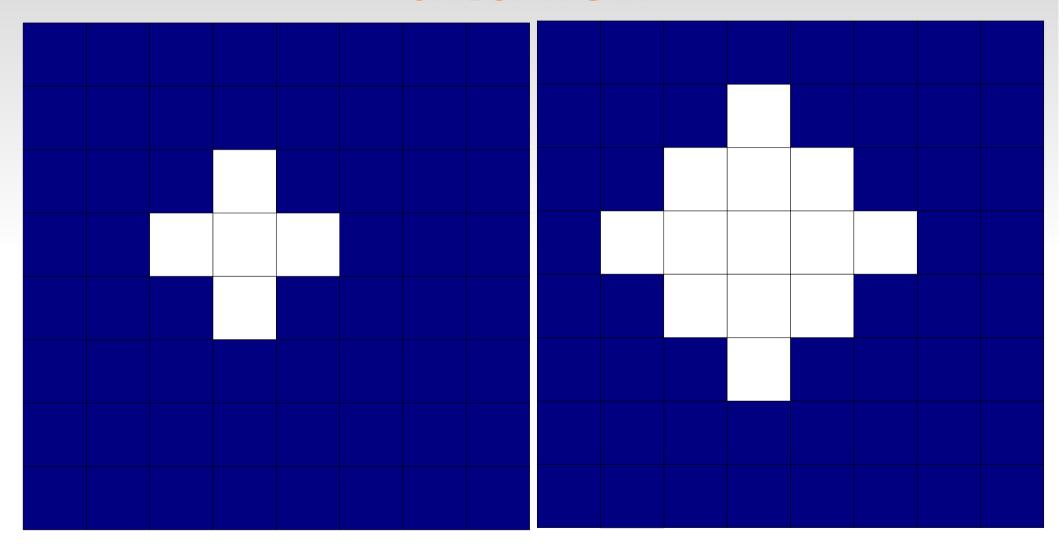


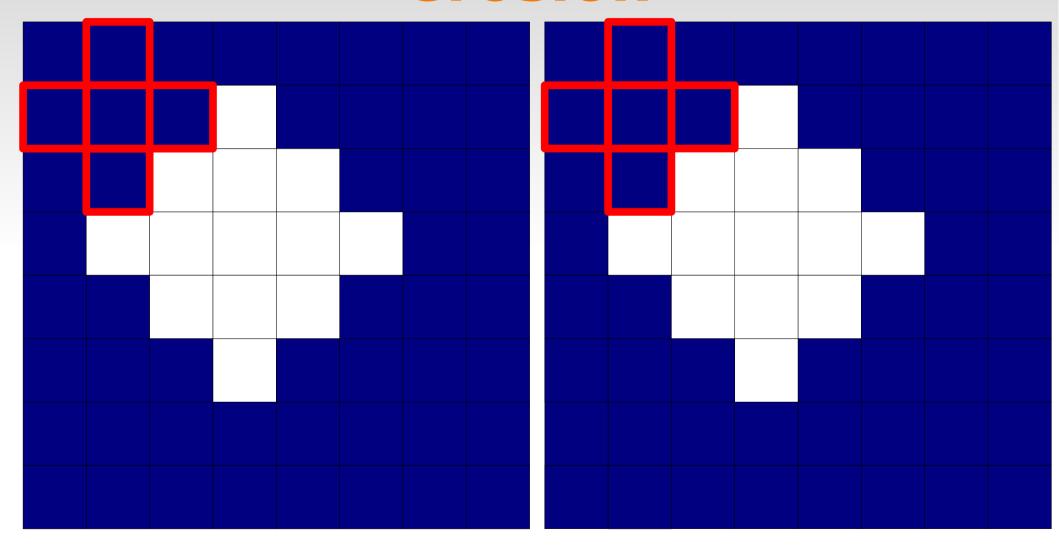


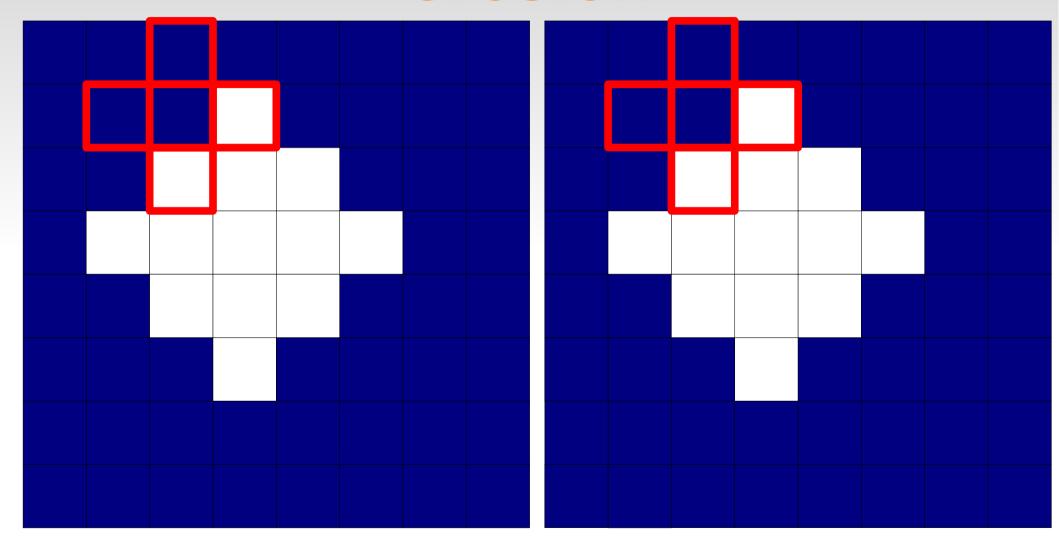


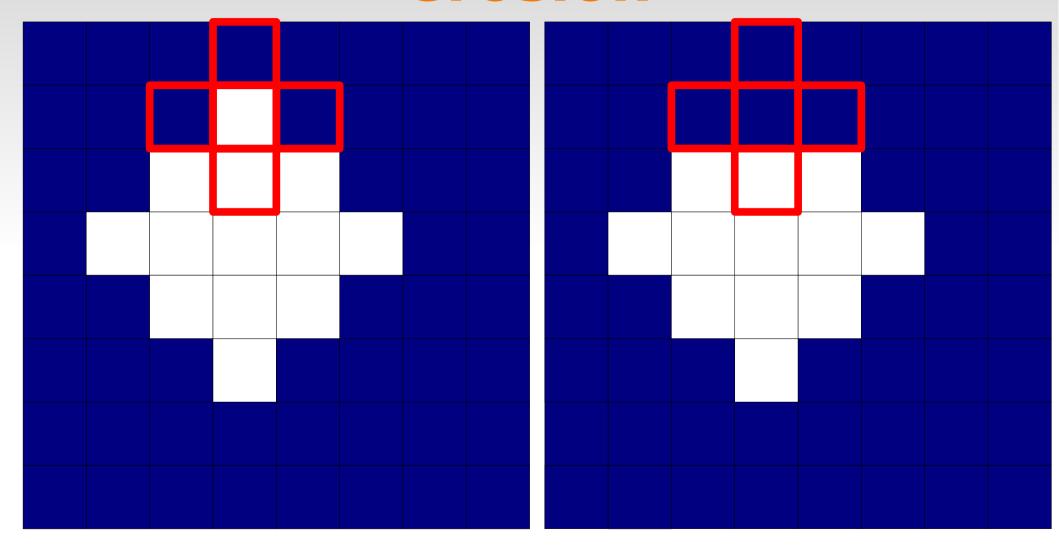


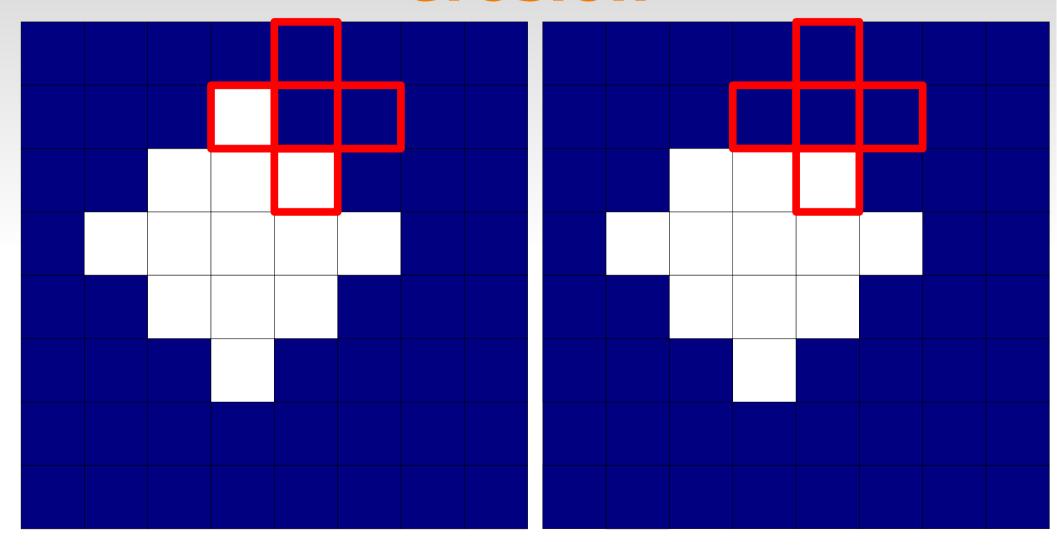


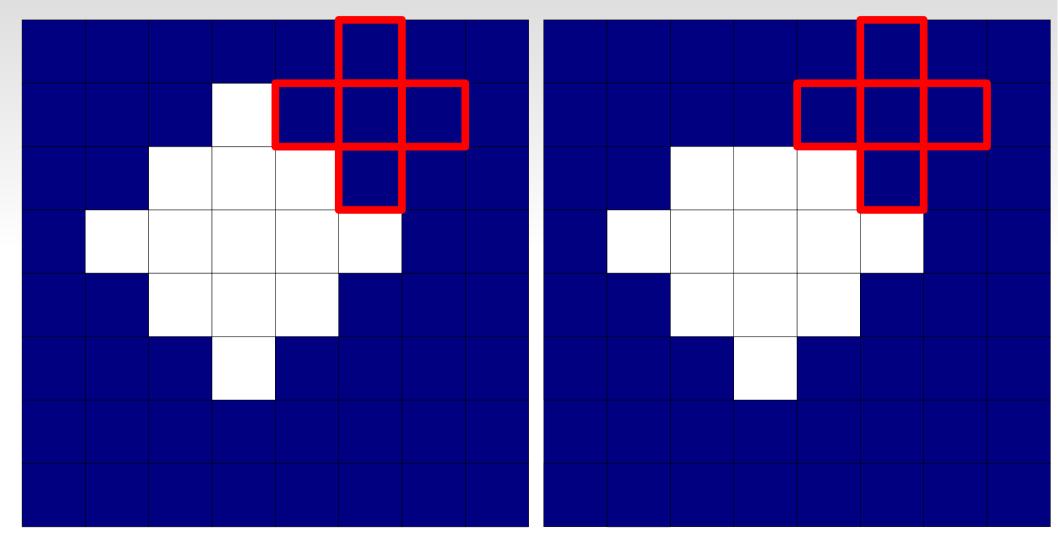


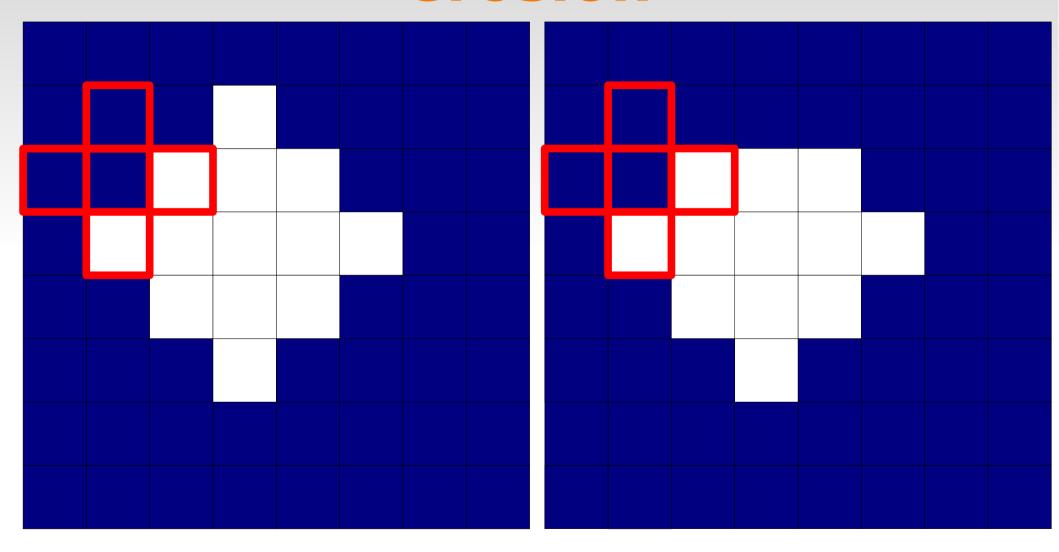


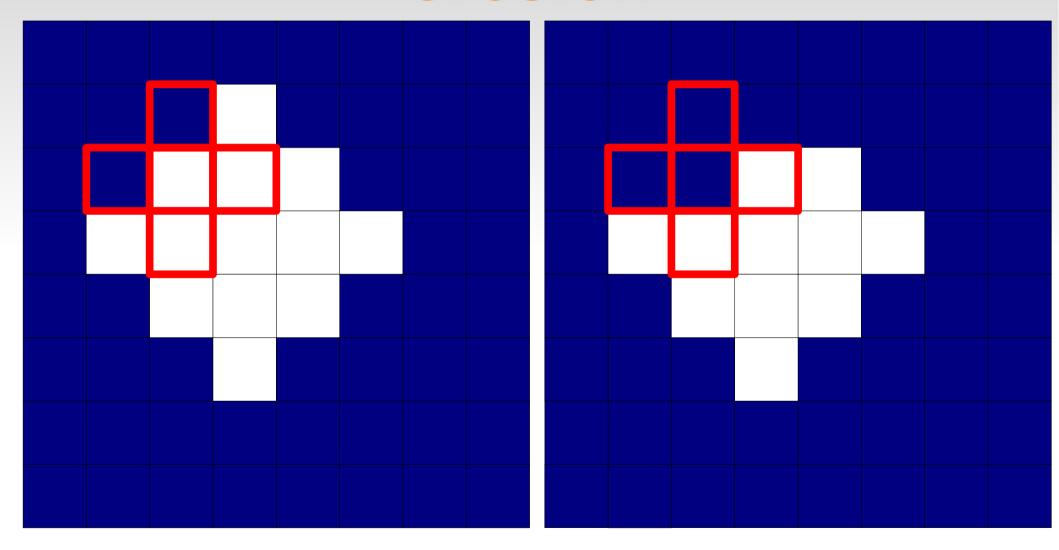


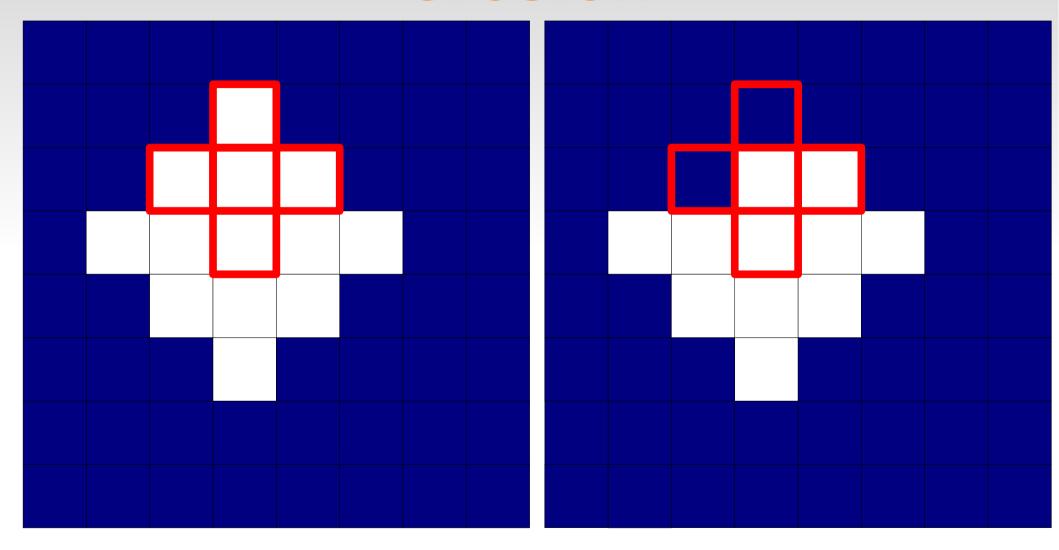


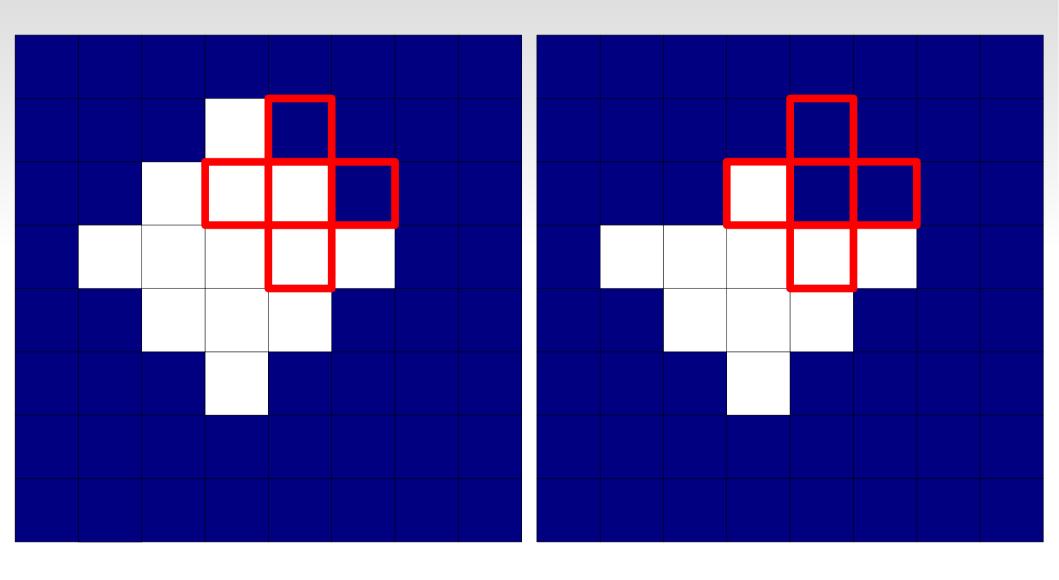


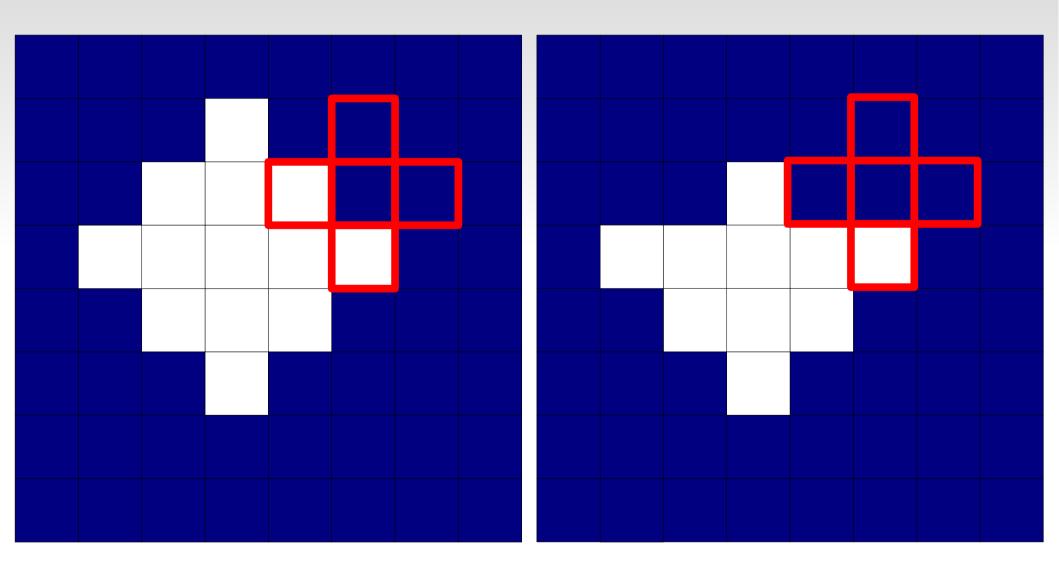


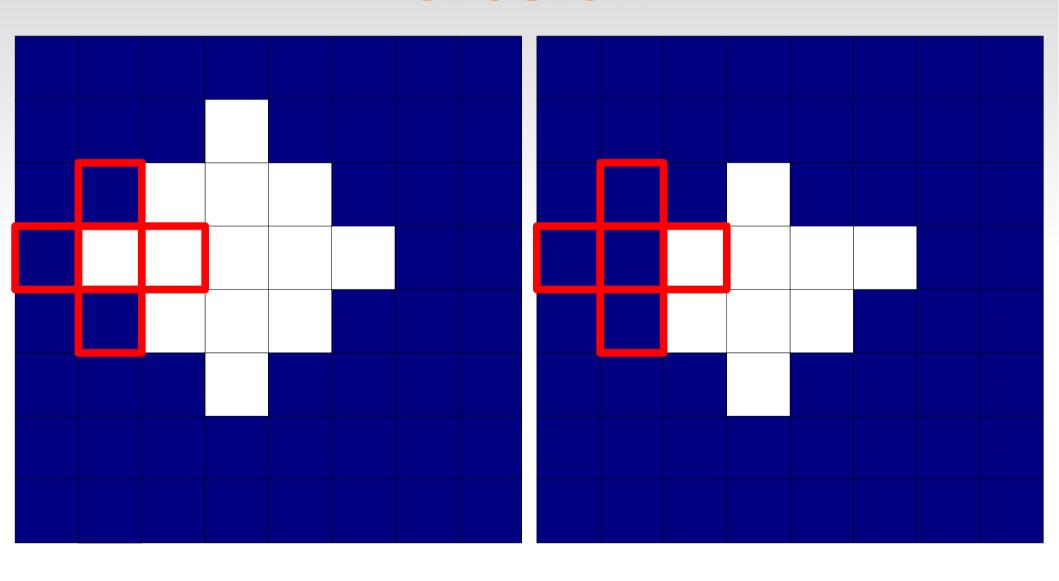


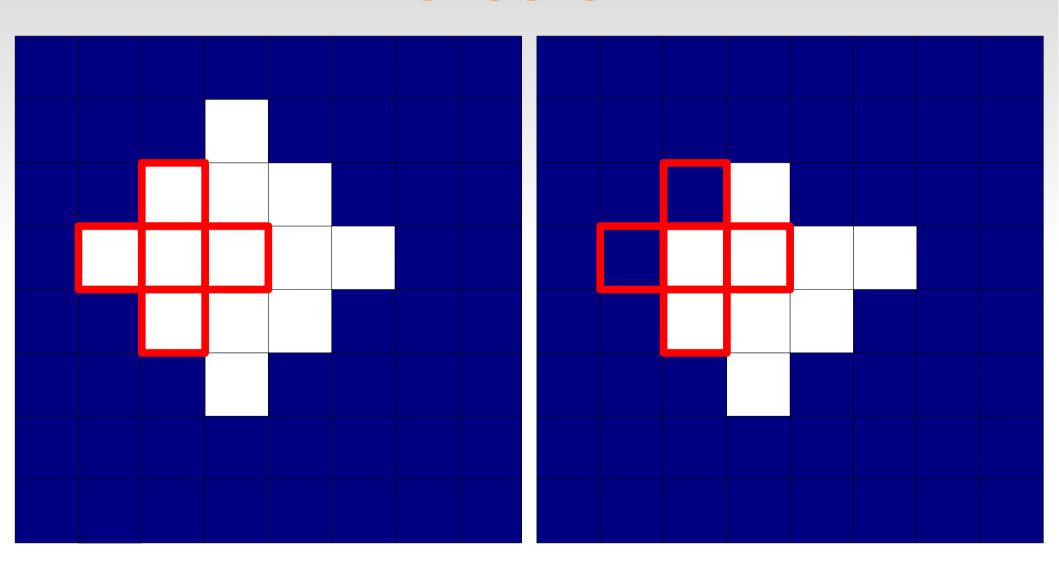


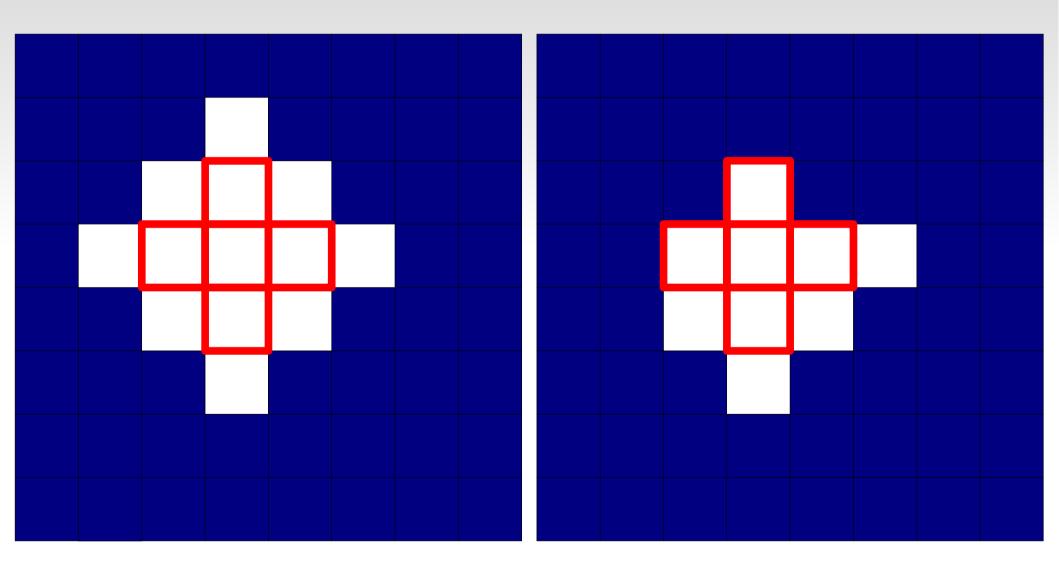


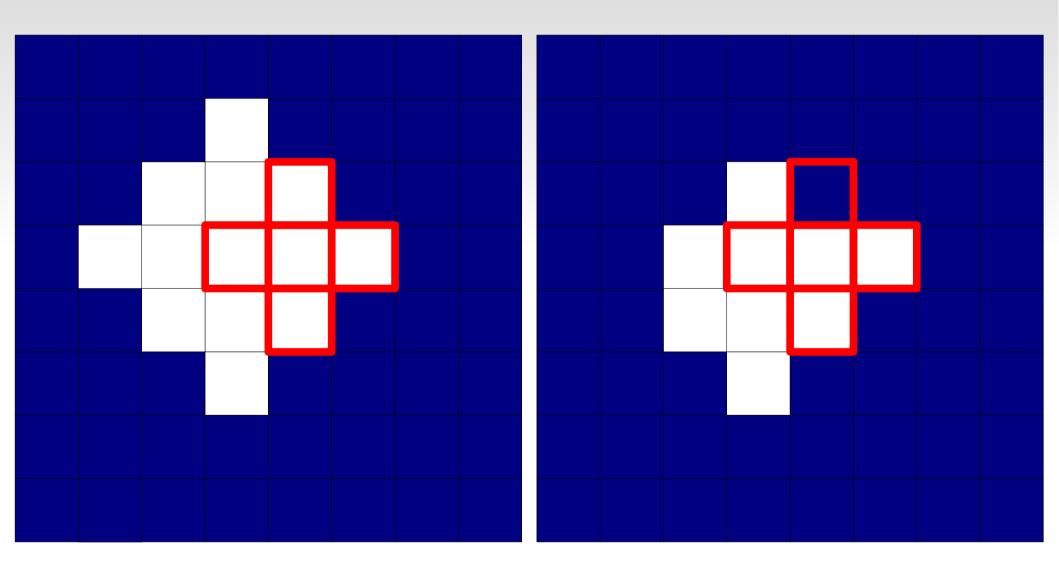


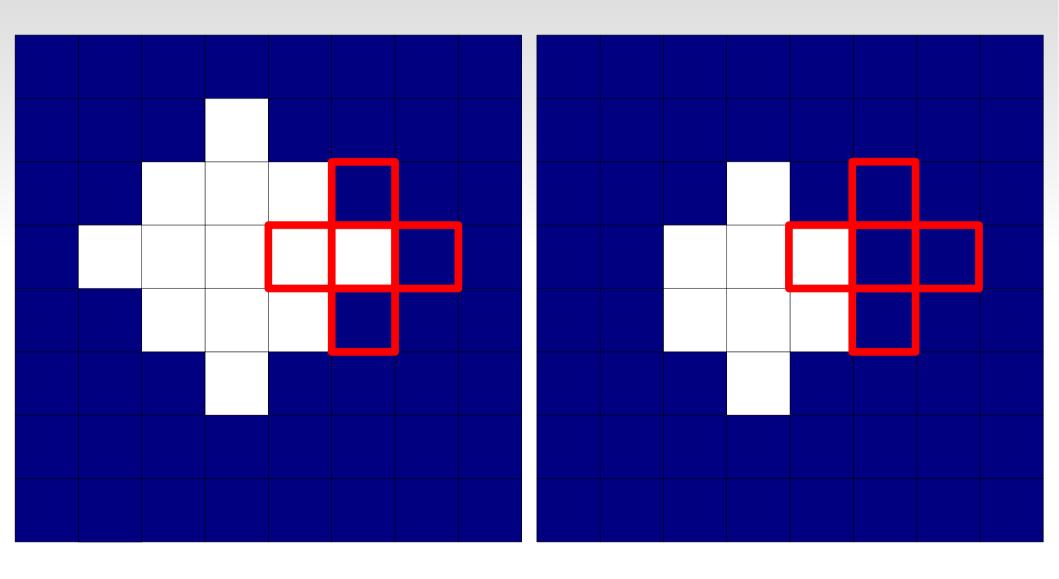


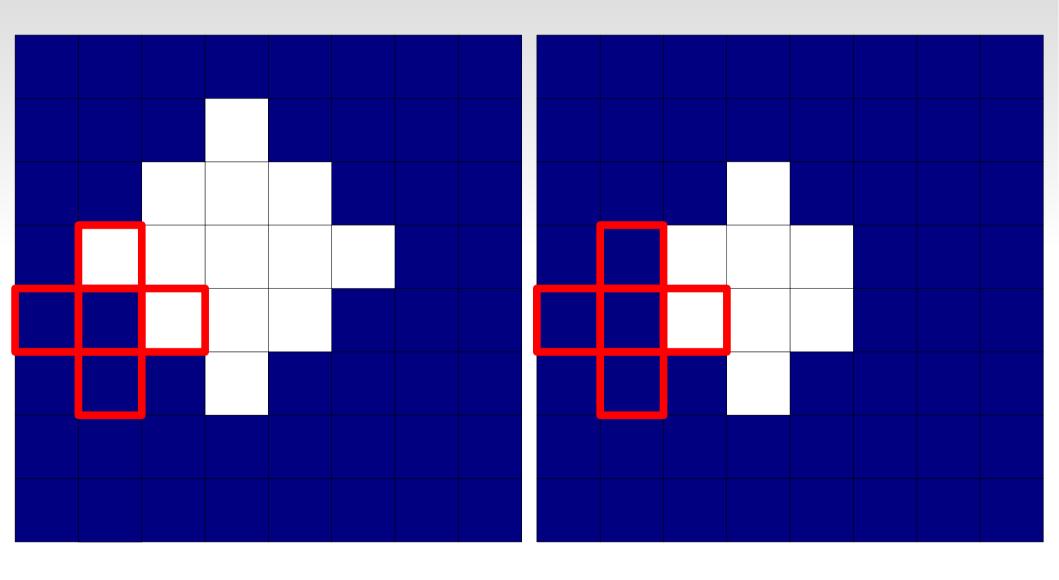


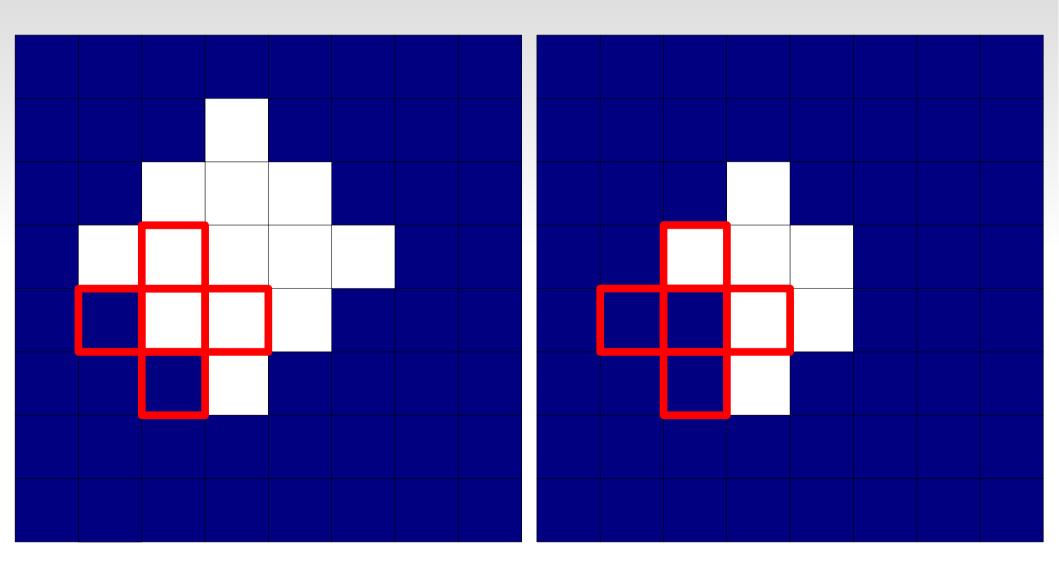


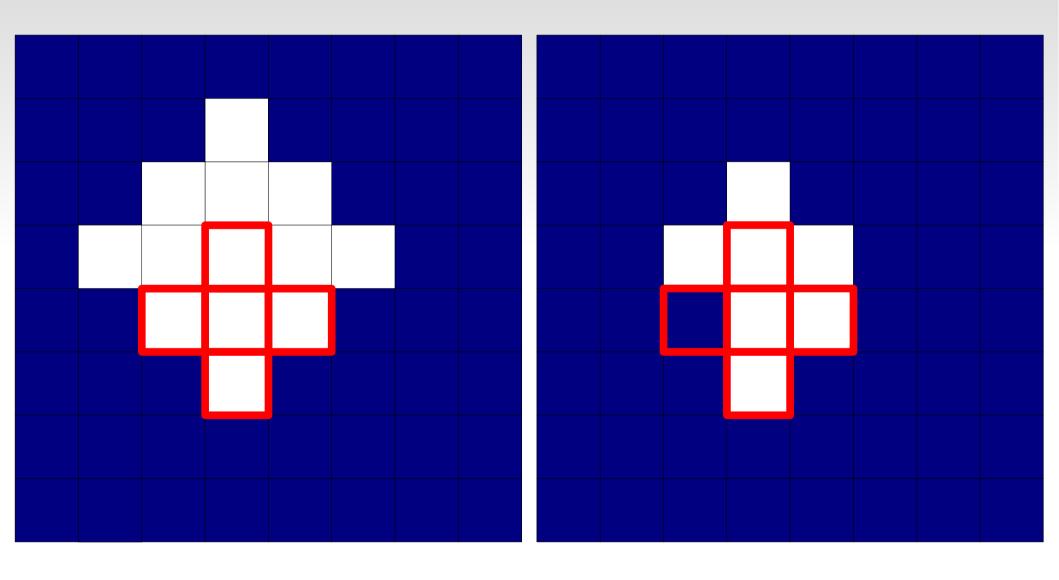


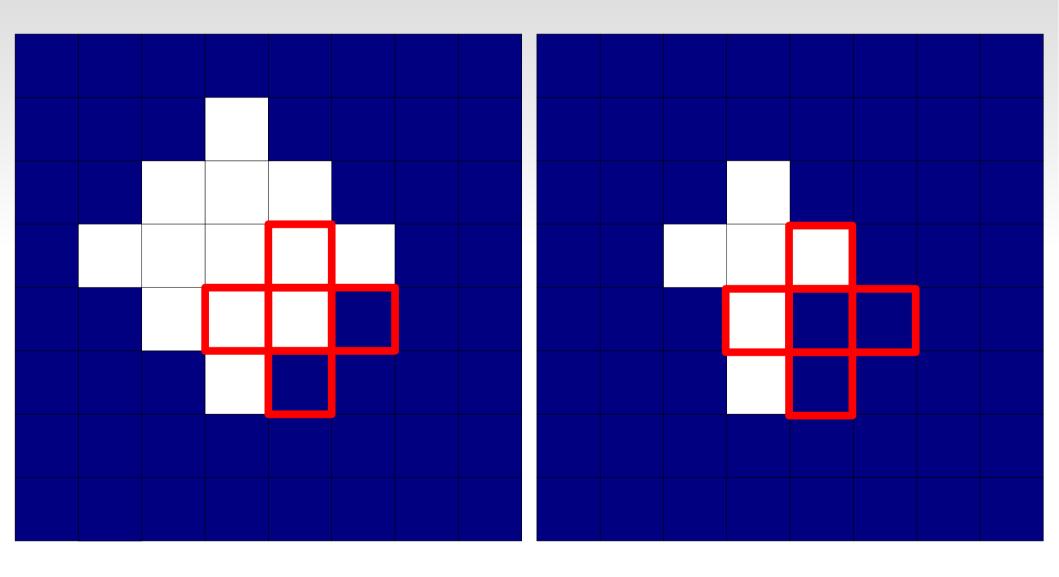


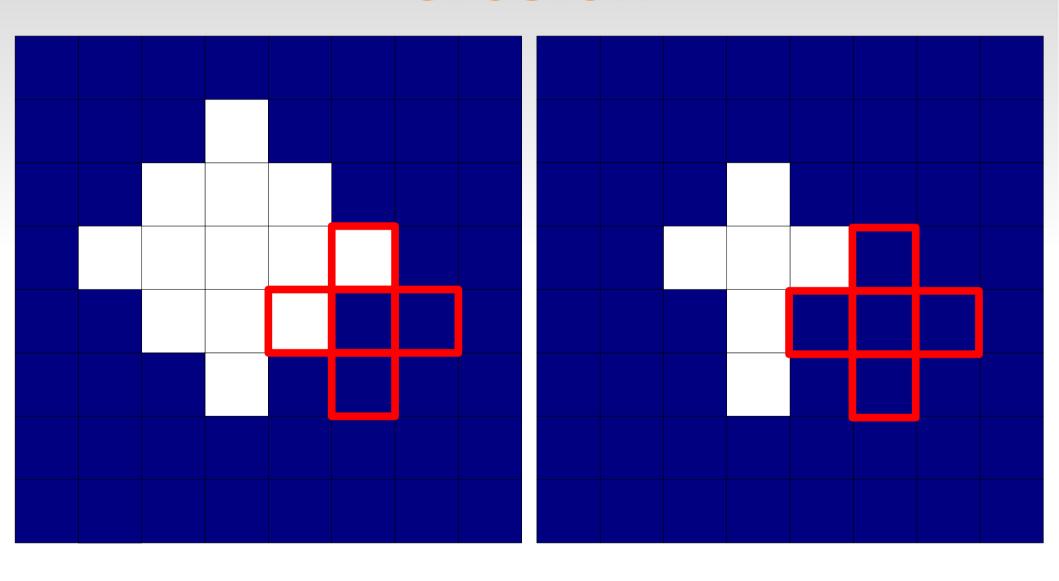


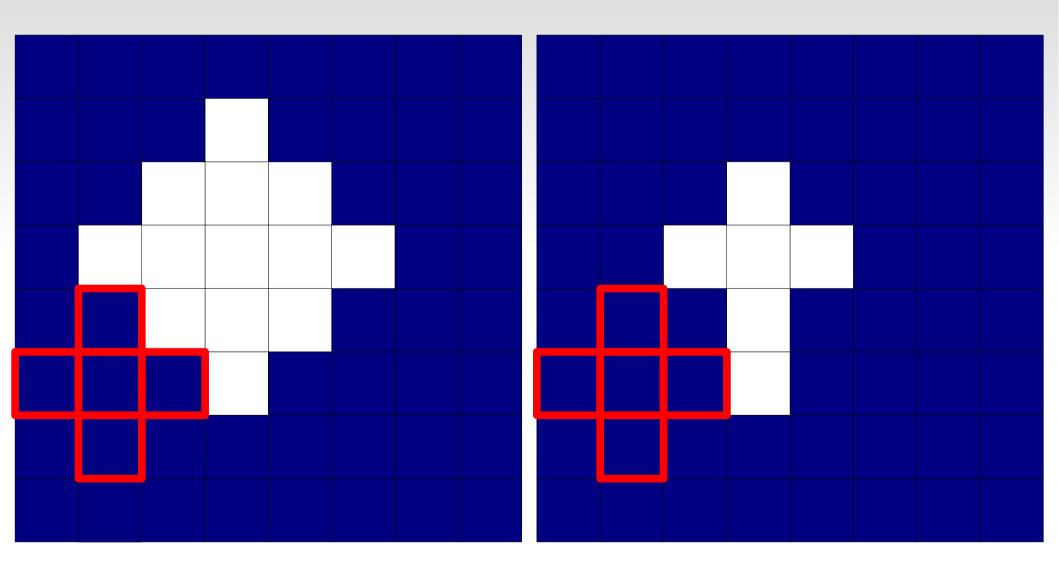


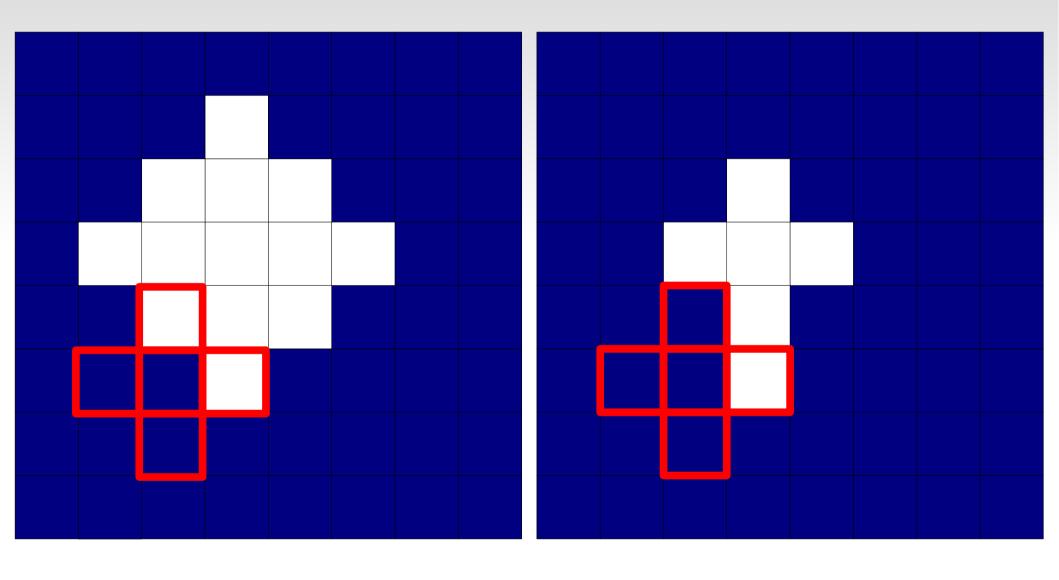


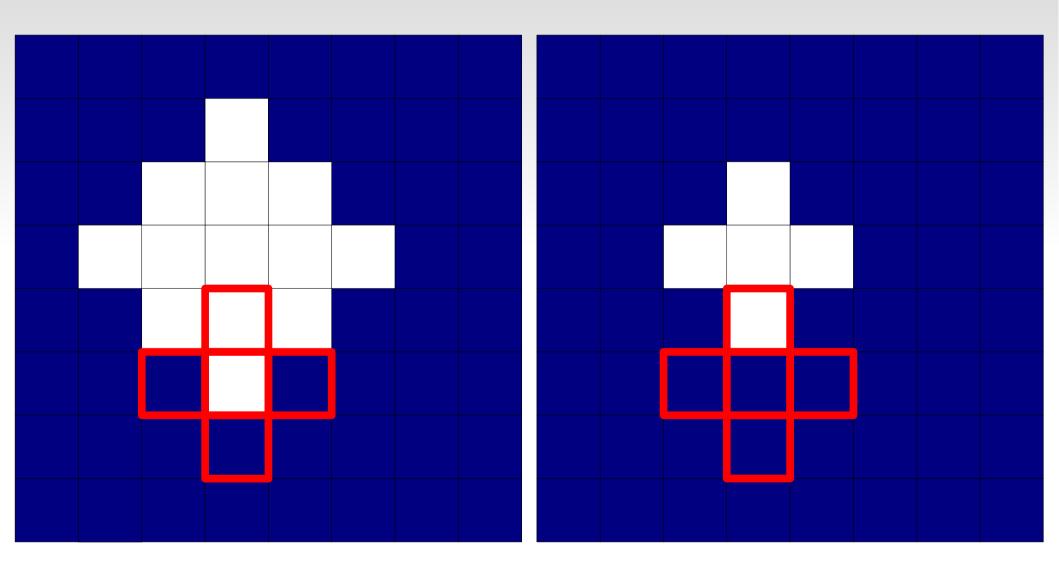


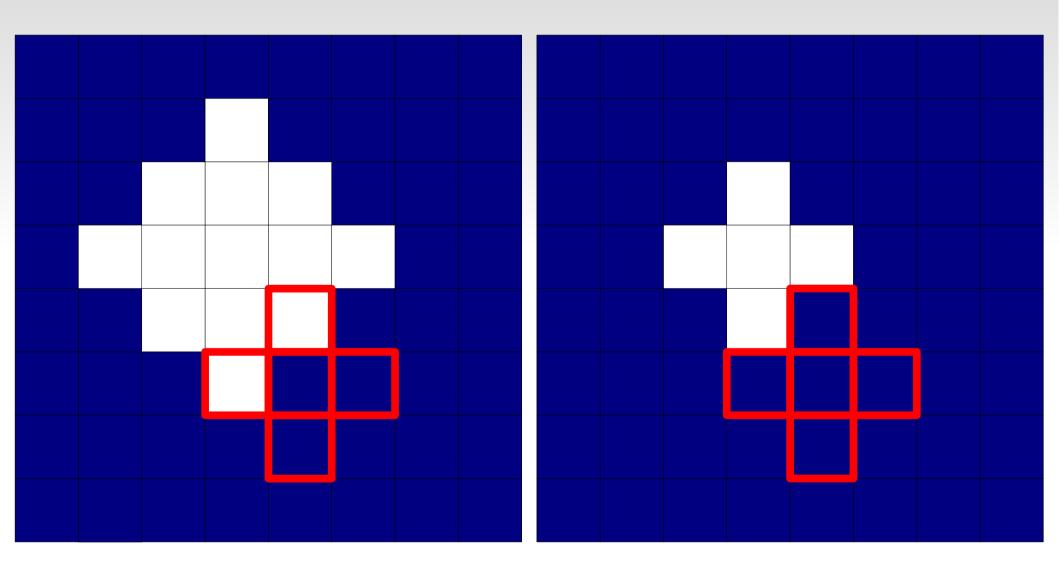


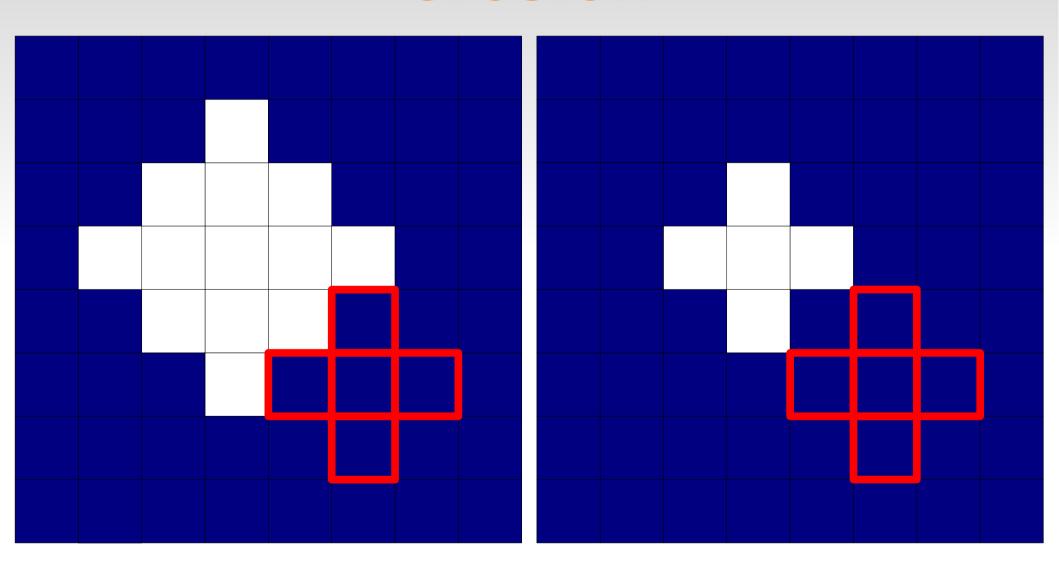


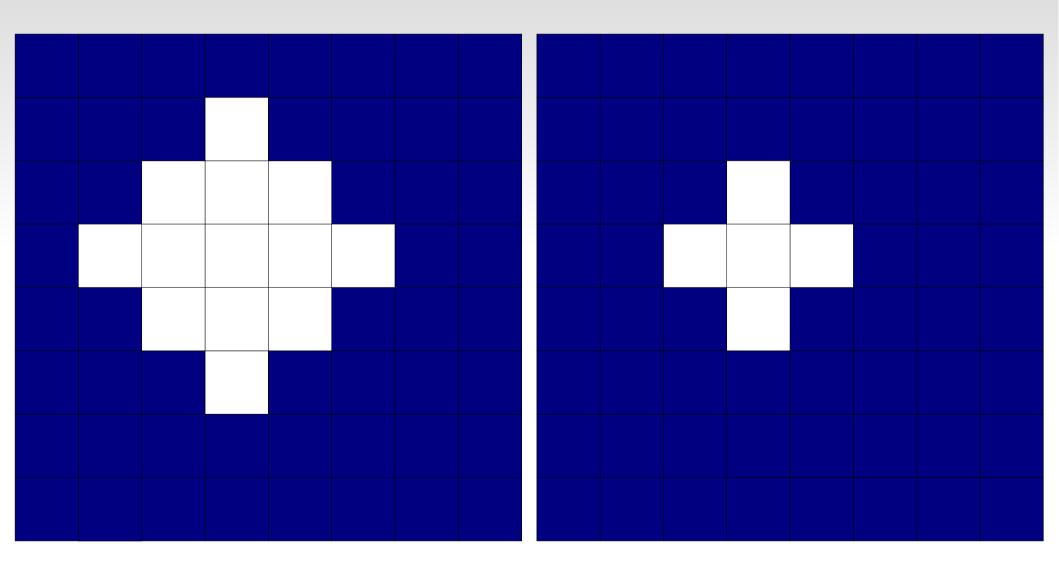




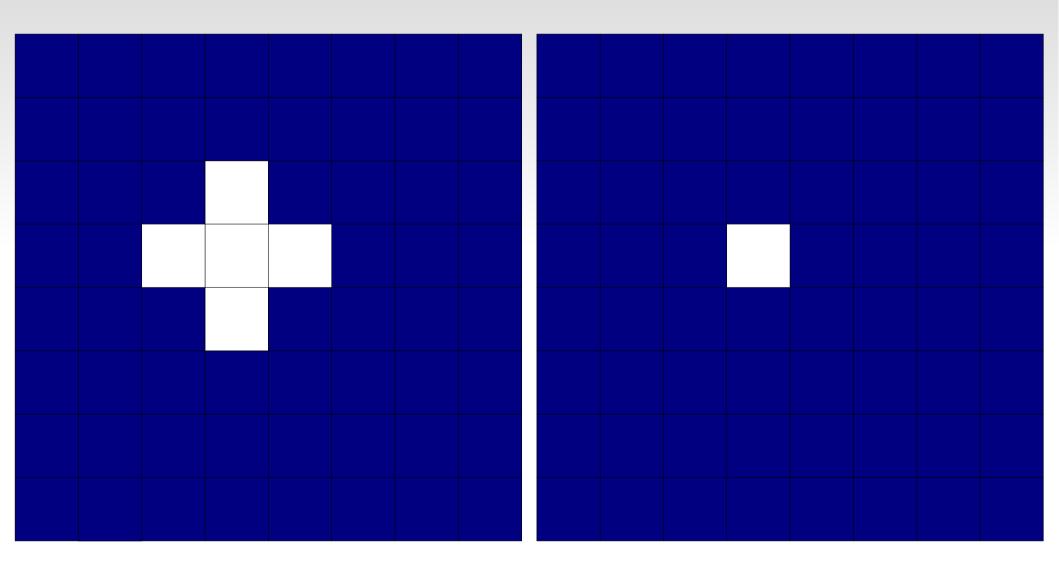




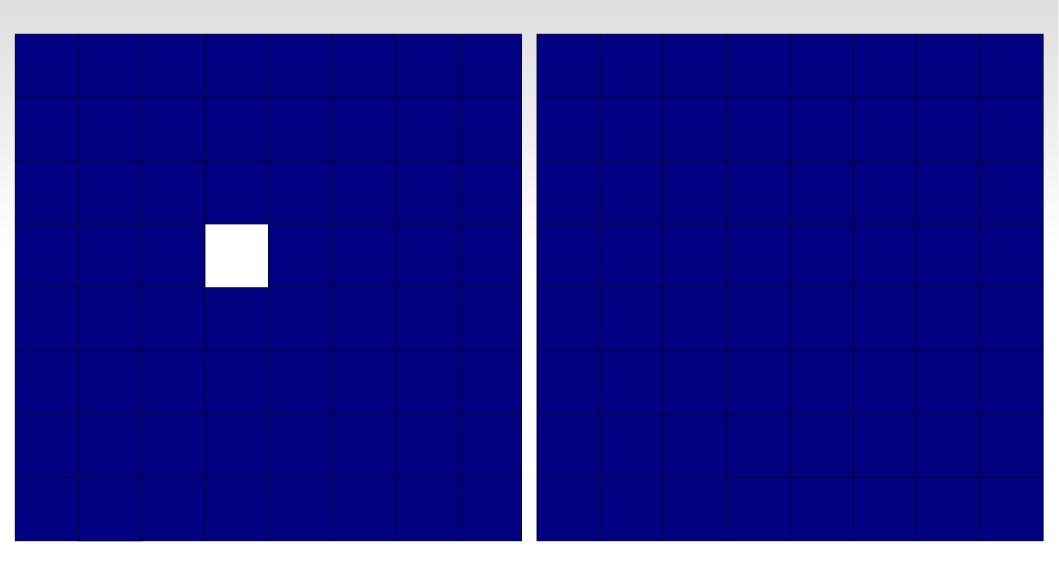




Binary Morphology - erosion

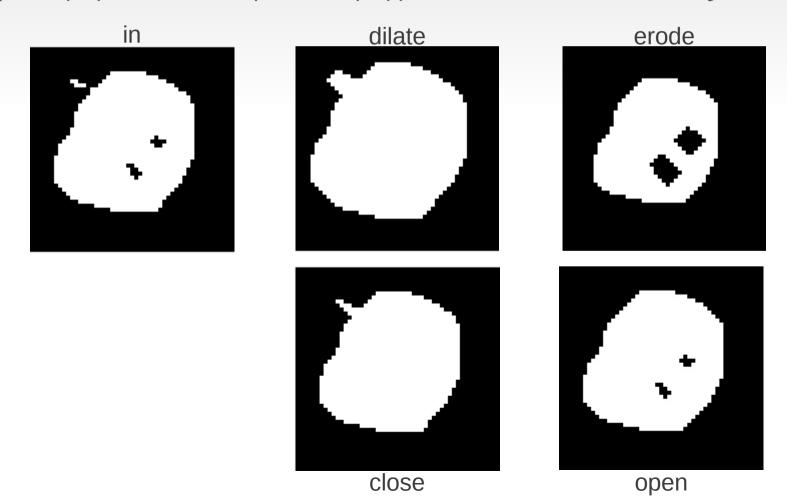


Binary Morphology - erosion



Binary Morphology - open and close

- close(X) = dilate(erode(X)) close holes in objects
- open(X) = erode(dilate(X)) remove small objects

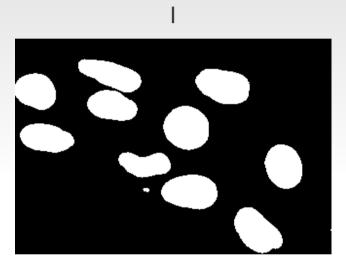


Binary Morphology - applications

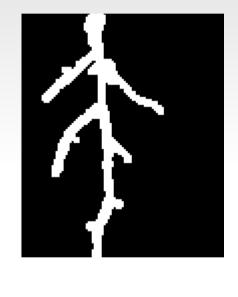
edge detection

skeletonization

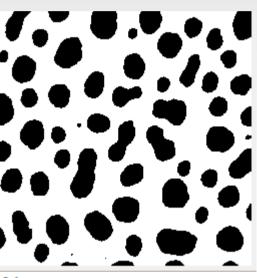
granulometry

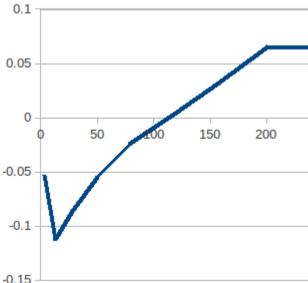


dilate(I) - erode(I)



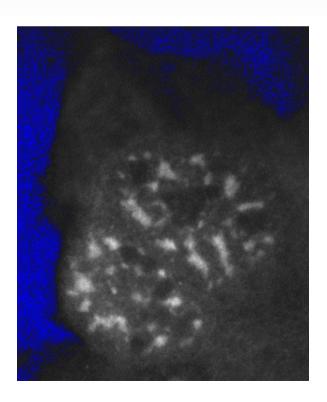


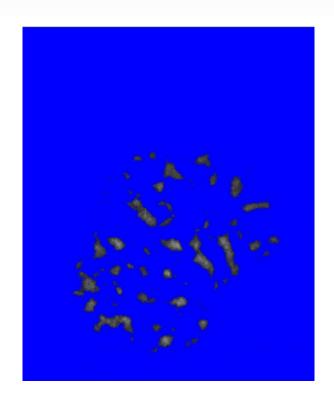




grayscale morphology

- dilate max over structuring element
- erode min over structuring element
- Example: grayscale top-hat filter (I-open(I))





filtering in the frequency domain

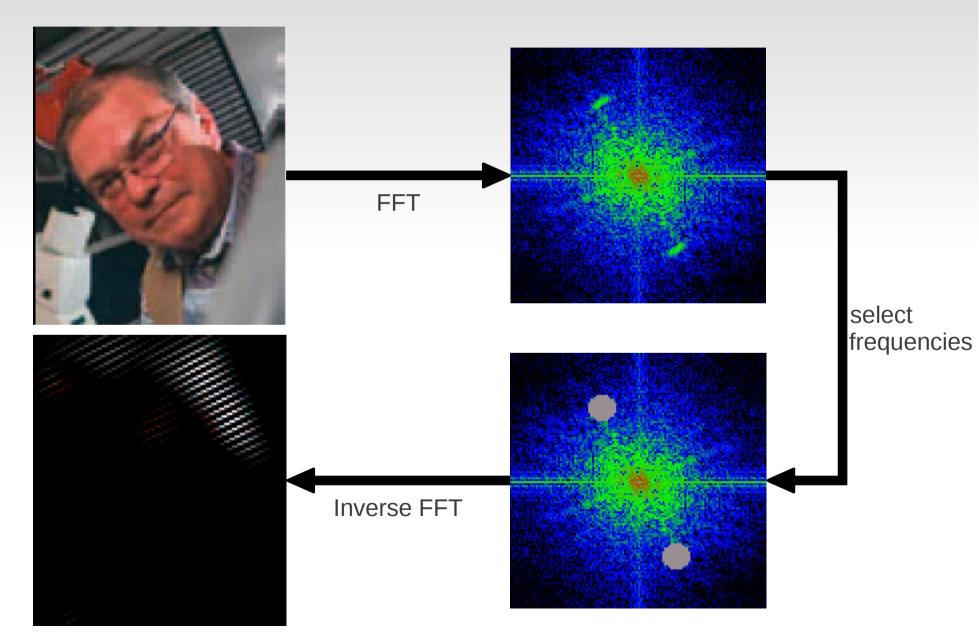
- Fourier Transform
- low-pass
- high-pass
- band-pass
- correlation
- convolution

filtering in the frequency domain - fourier transform

$$F(\mathbf{v}) = \int f(x) e^{-i2\pi v x} dx$$

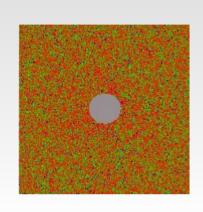
- signal can be represented as sum of sinoids
- FT transforms from spatial to frequency domain

Filtering in the frequency domain



Filtering in the frequency domain

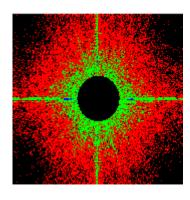




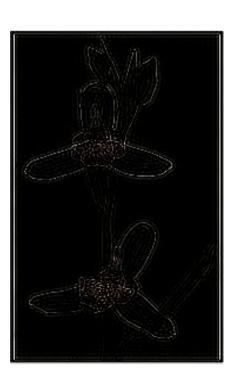
Low pass filter







High pass filter



Filtering in the frequency domain

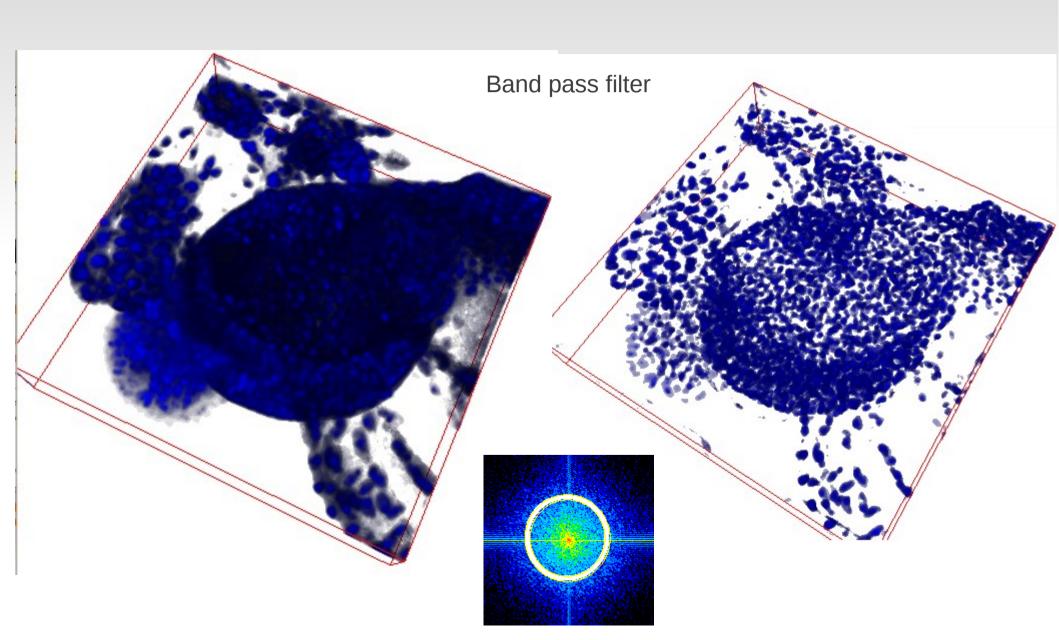
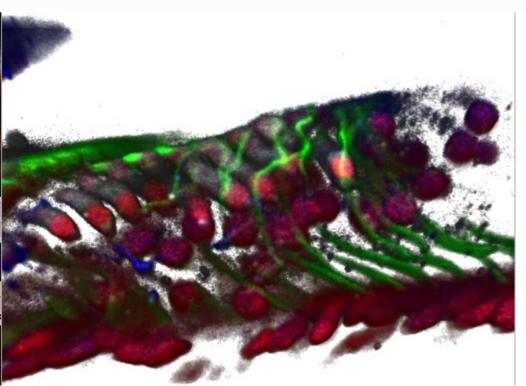


Image Restoration

- Image degraded
 - Noise
 - quantum nature of light (poisson distribution)
 - imperfect electronics (gaussian distribution)
 - Background
 - imperfect illumination
 - Blur
- out of focus light

Image Restoration - Noise reduction

- Mean Filter, Gaussian filter, Median filter
- Nonlinear diffusion filtering (anisotropic diffusion, Perona–Malik)
 - Smooth noise while keeping edges



- pde based approach
- inhomogeneous process that reduces the diffusivity at those locations which have a larger likelihood to be edges

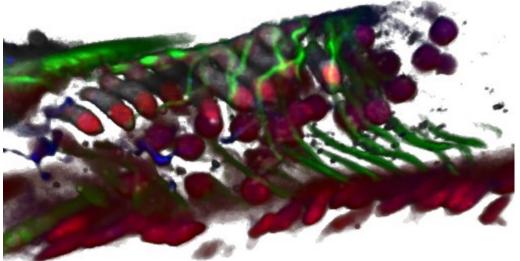
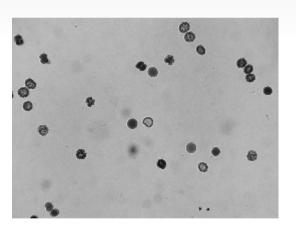


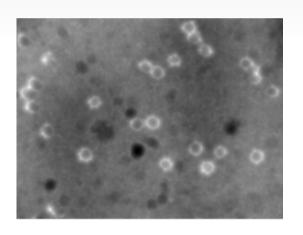
Image Restoration - **S**Background subtraction

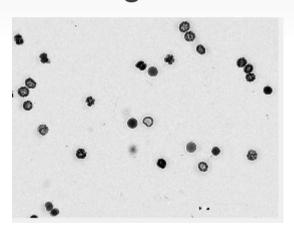
- correct inhomogenous illumination
 - correct with image of background

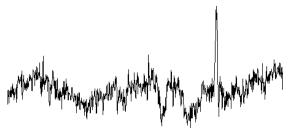
$$\frac{I}{B}$$
·mean (B)

if not available: estimate background image









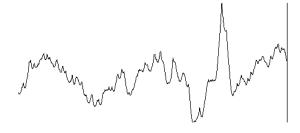
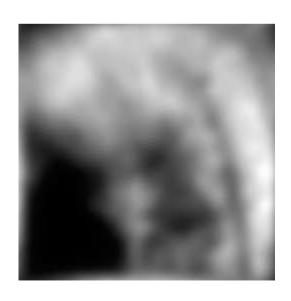
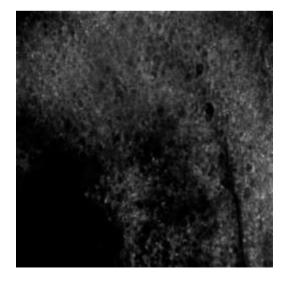


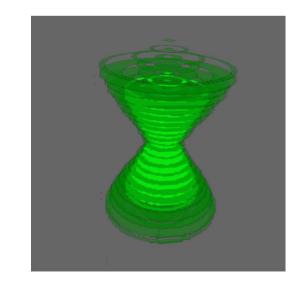


Image Restoration - Deconvolution

- blur
 - diffraction
 - out-of-focus light
- acquired image = object function convolved with psf

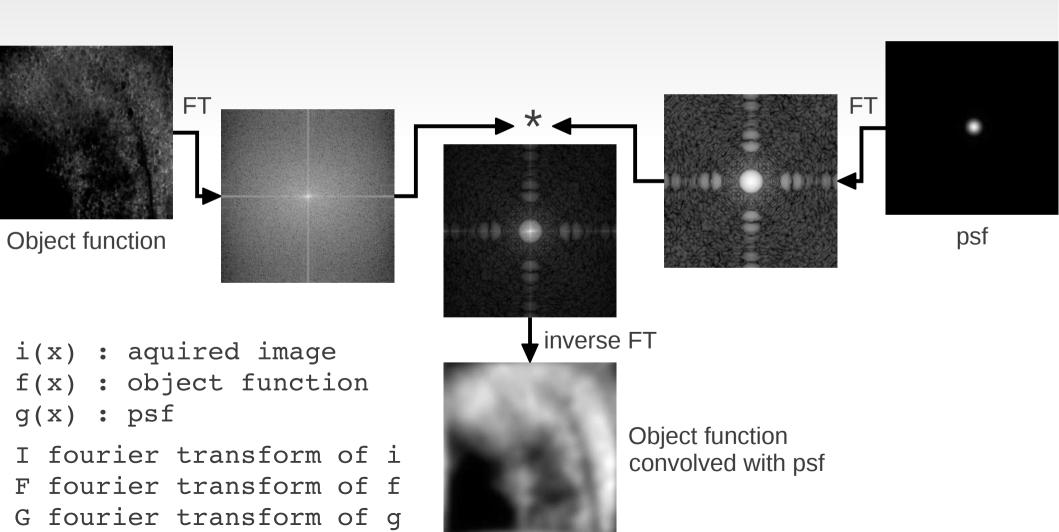






Deconvolution - Convolution theorem

$$i(x) = \int f(x') *g(x-x') dx \iff I = F *G$$



Deconvolution

$$i(x) = \int f(x') * g(x-x') dx'$$
 <=> $I = F * G$

- Deconvolution: find object function f for given image i and psf g
- Unfortunatly it is not practicable to compute

$$F = \frac{I}{G}$$

- G has zeros outside certain regions
 - Setting F zero for these would create artefacts
- In practice there is noise

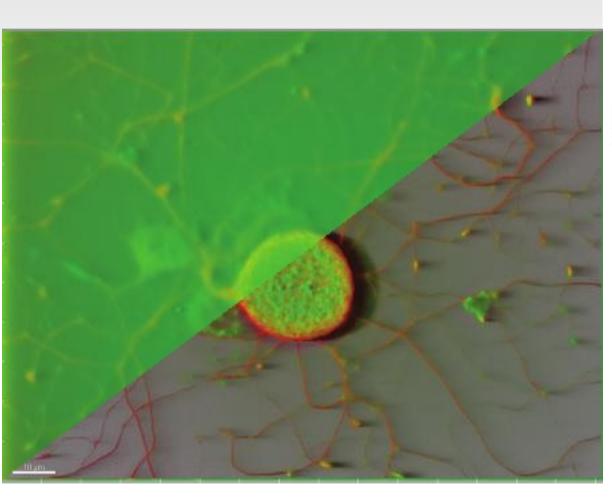
$$I = F * G + N$$

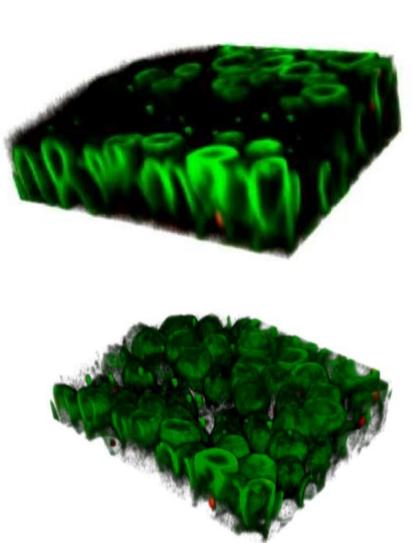
- N/G would amplify noise
- It's not possible to reconstruct the real object function

Deconvolution algorithms

- Solution
 - Find an algorithm that computes a function f' so that
 - f' estimates f as good as possible
 - works in the presence of noise
- Different deconvolution algorithms exist
- In general best for fluorescent microscopy:
 - (Classical) Maximum Liklihood Estimation MLE

Deconvolution - examples





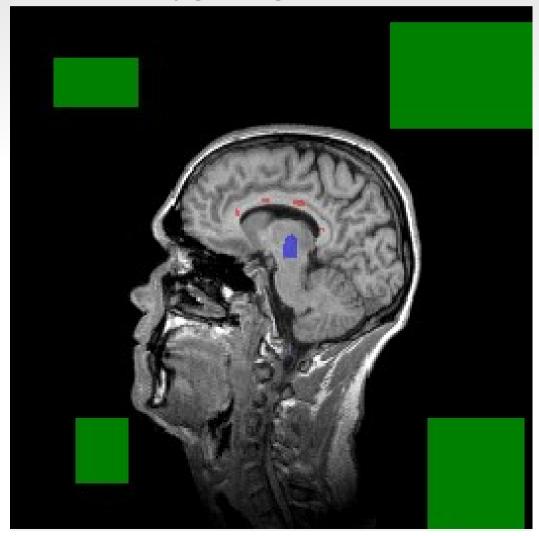
Segmentation

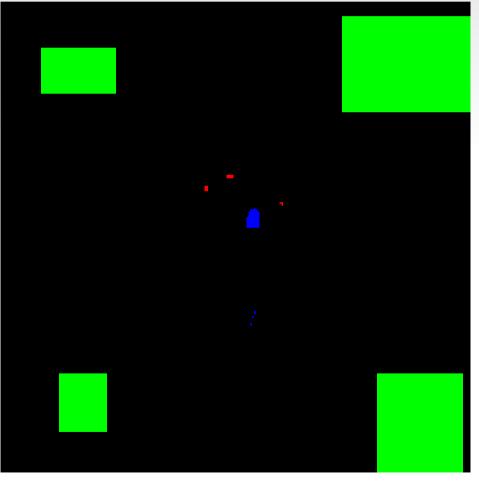
- separate objects from background and objects from each other
 - region growing
 - clustering
 - watershed transform

Segmentation - region growing

- start from seed-points
- simultaneously grow regions

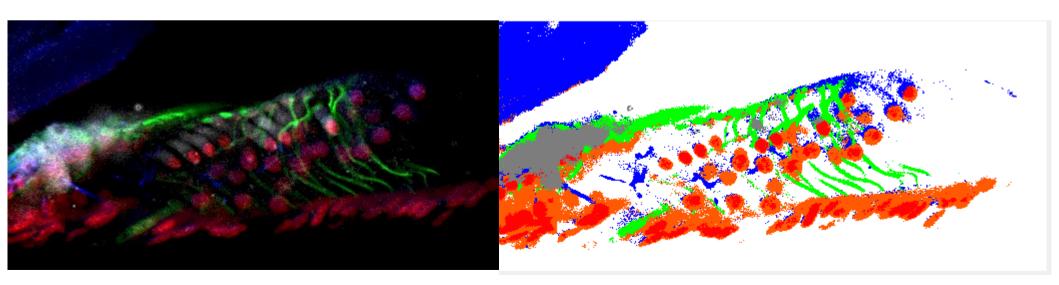
stop according to a homogenity criterium



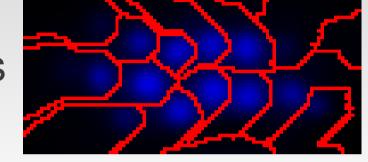


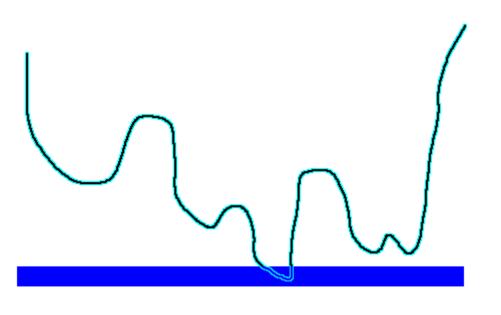
Segmentation - clustering

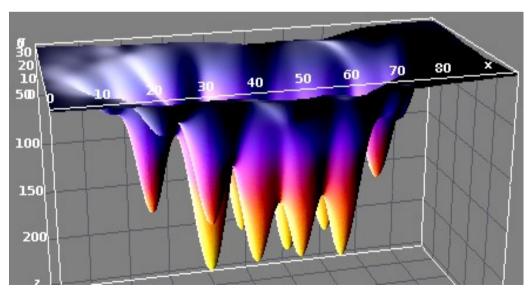
- k-means clustering
 - interpret channel values as coordinate vectors in space
 - partition space around mean values into k-clusters
 - iterative, optimization algorithm



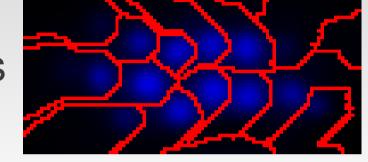
- interpret intensity as valleys
- fill slowly with rising water

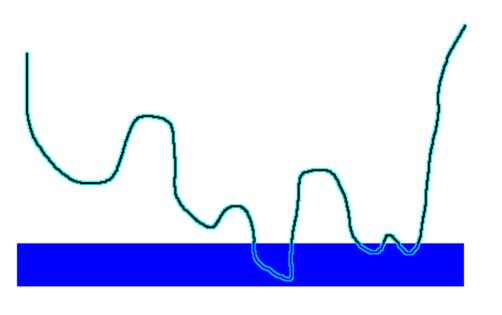


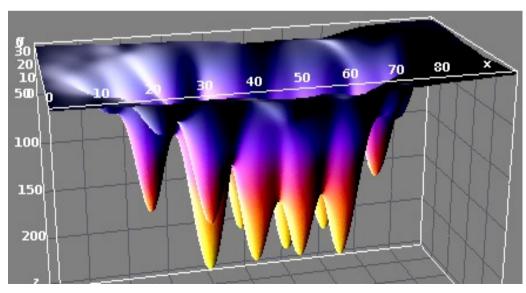




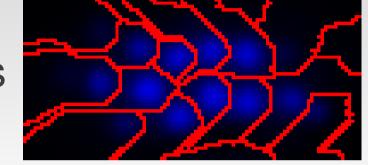
- interpret intensity as valleys
- fill slowly with rising water

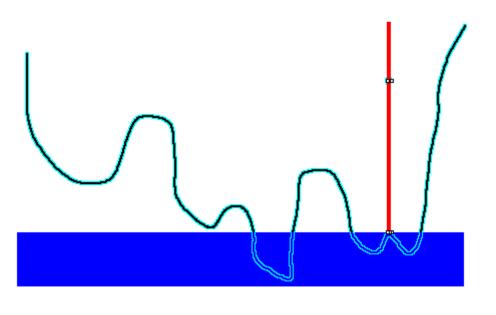


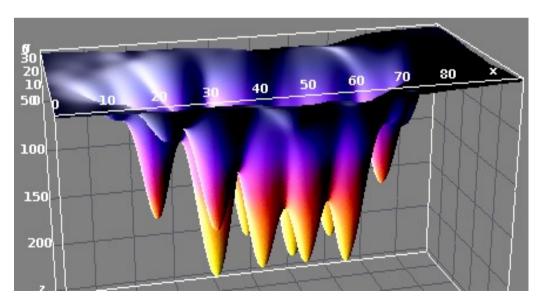




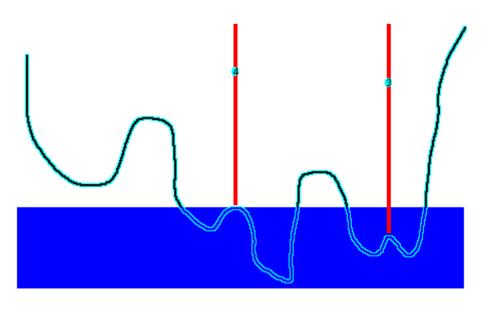
- interpret intensity as valleys
- fill slowly with rising water

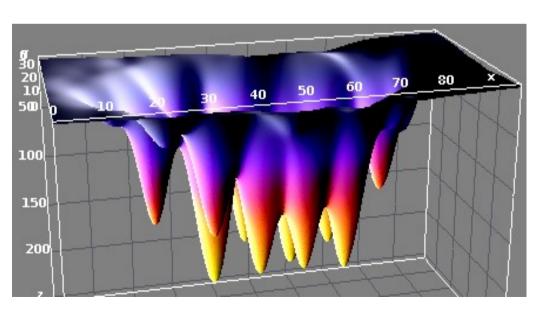


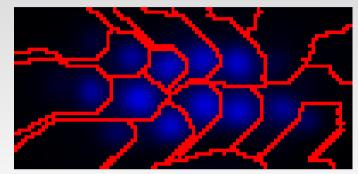




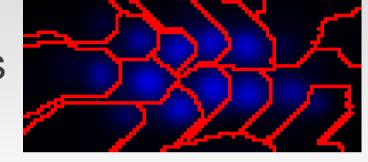
- interpret intensity as valleys
- fill slowly with rising water
- whenever two basins join create a separation

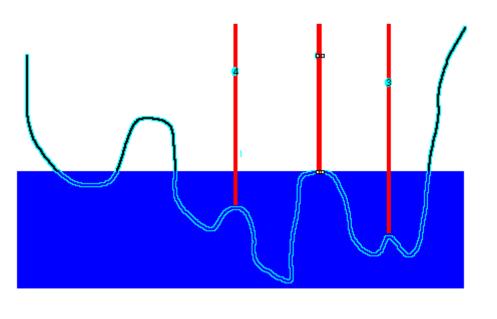


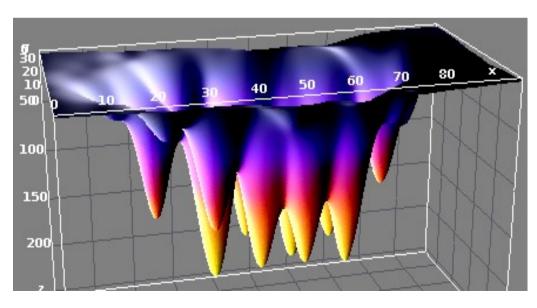




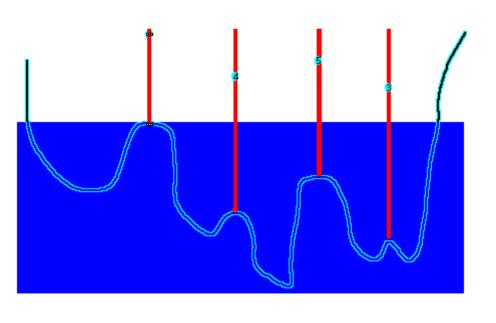
- interpret intensity as valleys
- fill slowly with rising water

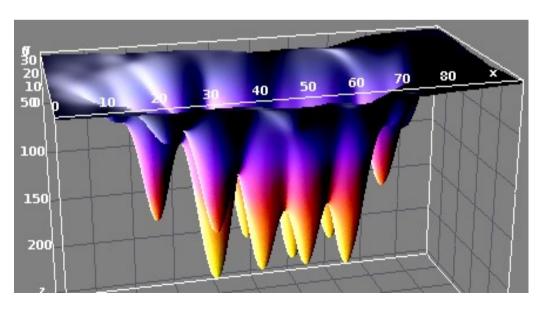






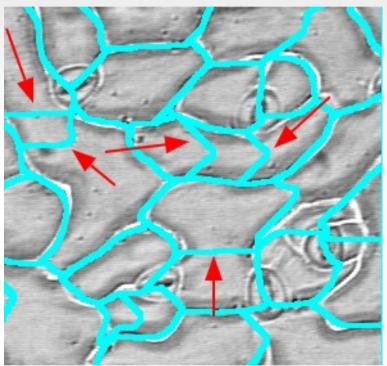
- interpret intensity as valleys
- fill slowly with rising water
- whenever two basins join create a separation





problem: over-segmentation





possible solution: seeded watershed

number of final basins = number of seeds

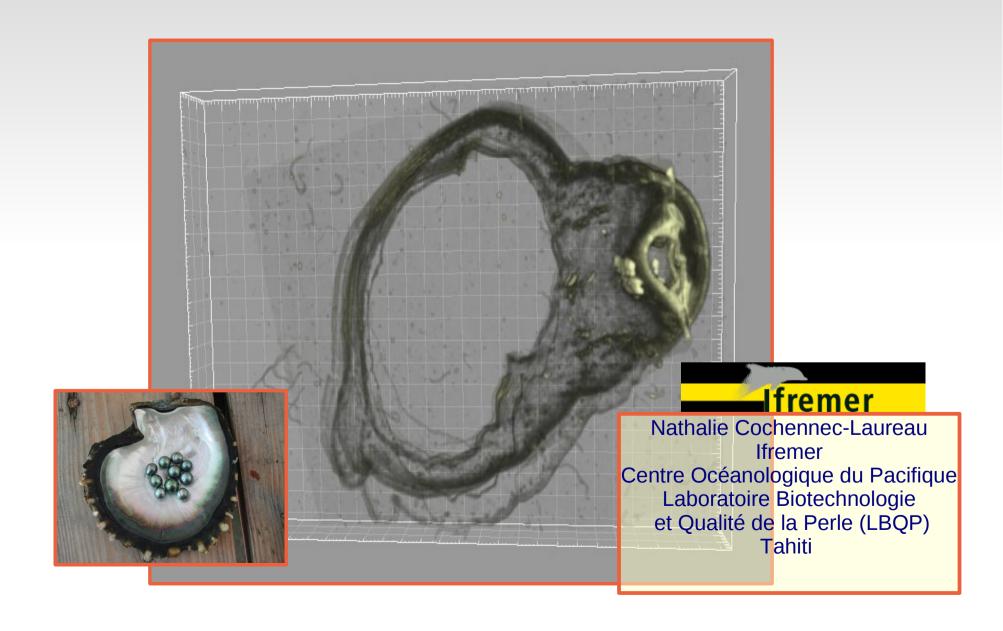
Geomectrical Transformation

- problem:
 - image is spatially distorted or
 - mismatch between channels due to chromatic aberration
 - barrel distortion or pincushion distortion
 - speciman moved during acquisition
 - lacks spatial correspondence
 - histological slices
 - combining images from different sources
 - stitching of images of a mosaic
- solution:
 - image registration or alignment

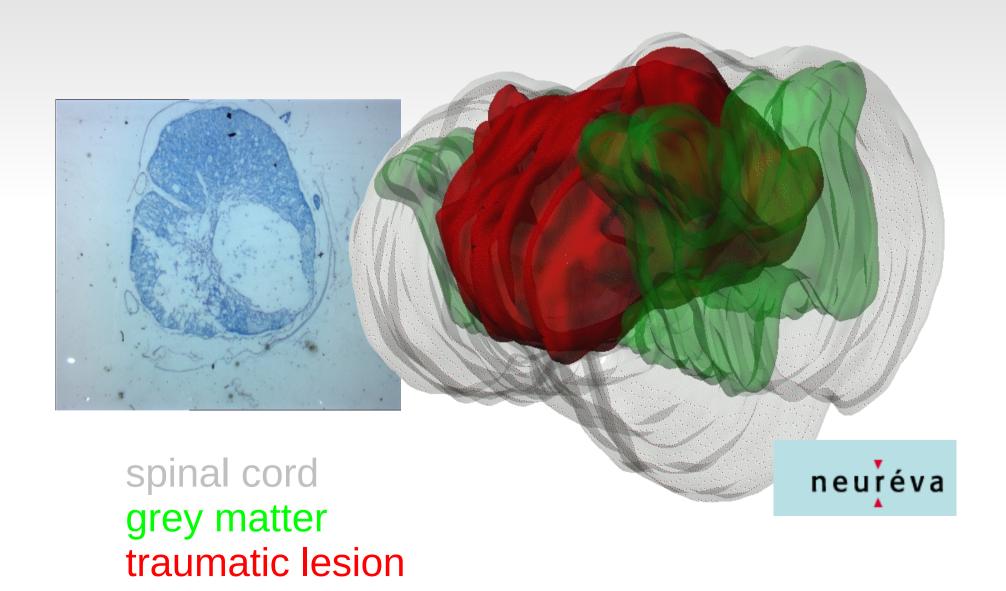
Image Registration

- Image registration
 - coordinate transformation
 - landmark based
 - manually selected
 - automtically extracted
 - intensity based
 - calculate match between images
 - possible transformations
 - rigid, affine, curved
 - resampling
 - interpolation
 - nearest neighbor, linear, cubic spline

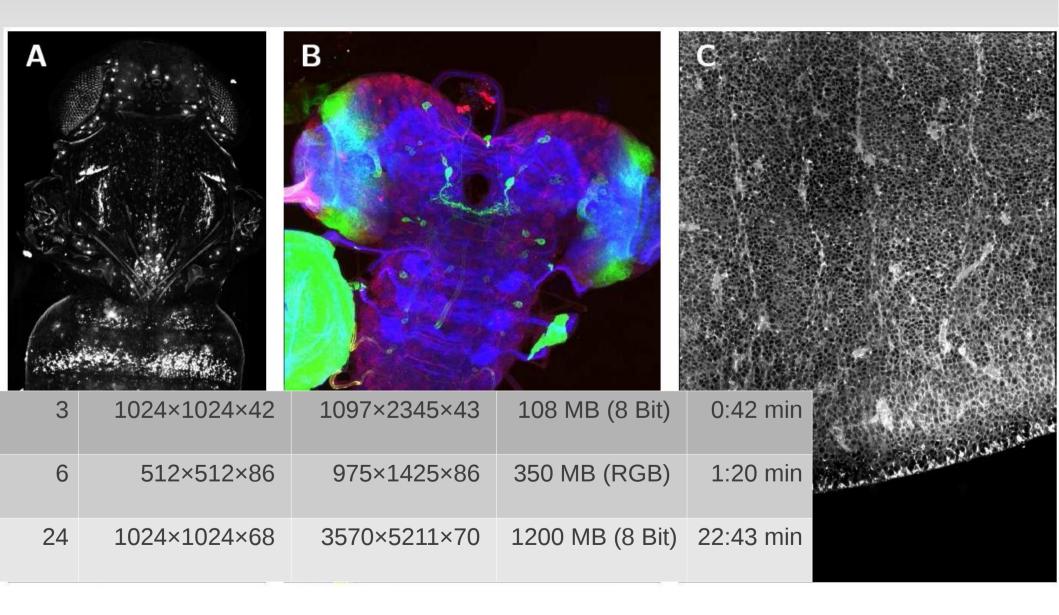
Example Registration



Example Registration



Example Stitching



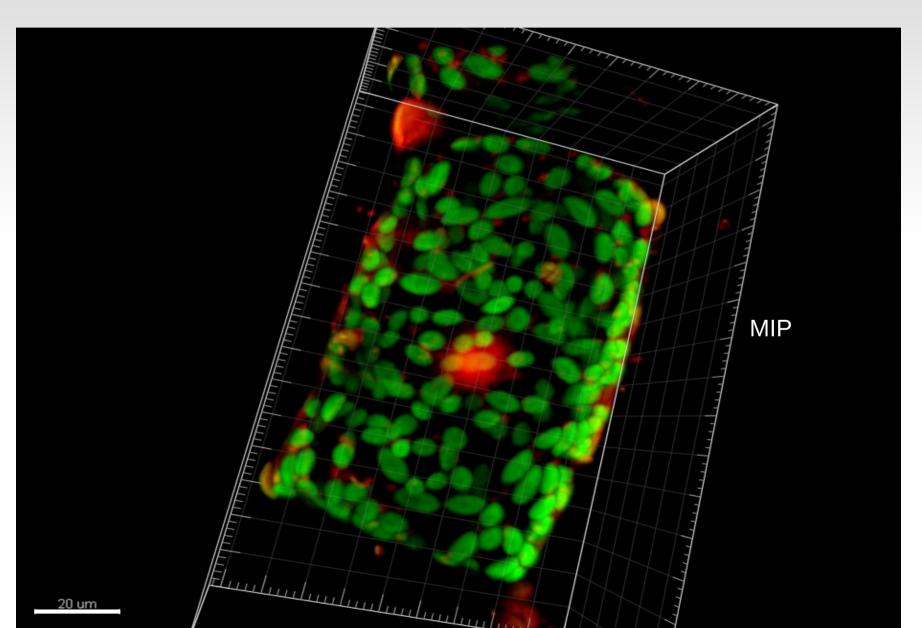
Visualization

- how to understand multidimensional data?
 - reduce dimensionality in a sensible way
- methods
 - volume rendering
 - methods that use the raw data directly without geometrical representation
 - ray tracing
 - maximum intensity projection (MIP)
 - blend (calculated from all information along the ray)
 - surface rendering
 - take into account only surfaces of objects
 - needs a description of the object in terms of geometrical entities

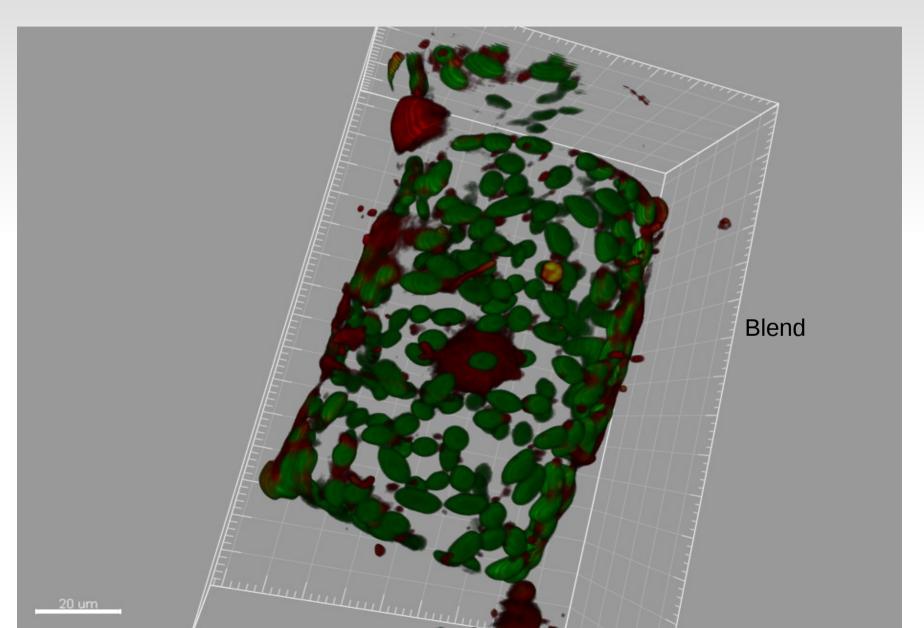
Visualization - Volume Rendering

- how does the volume interact with a ray of light
 - given position and parameters of the light source
 - given the position of the observer

Visualization - Volume Rendering



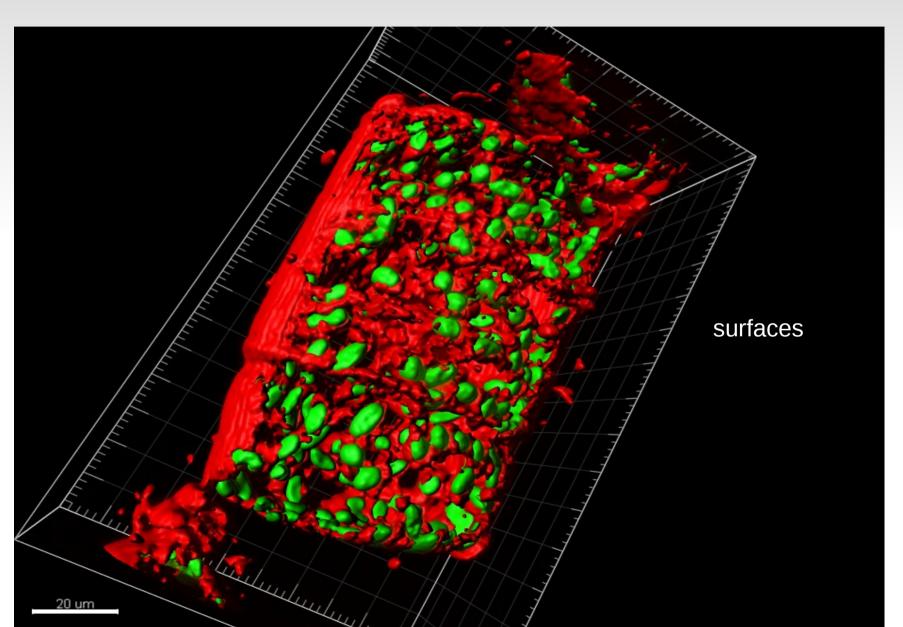
Visualization - Volume Rendering



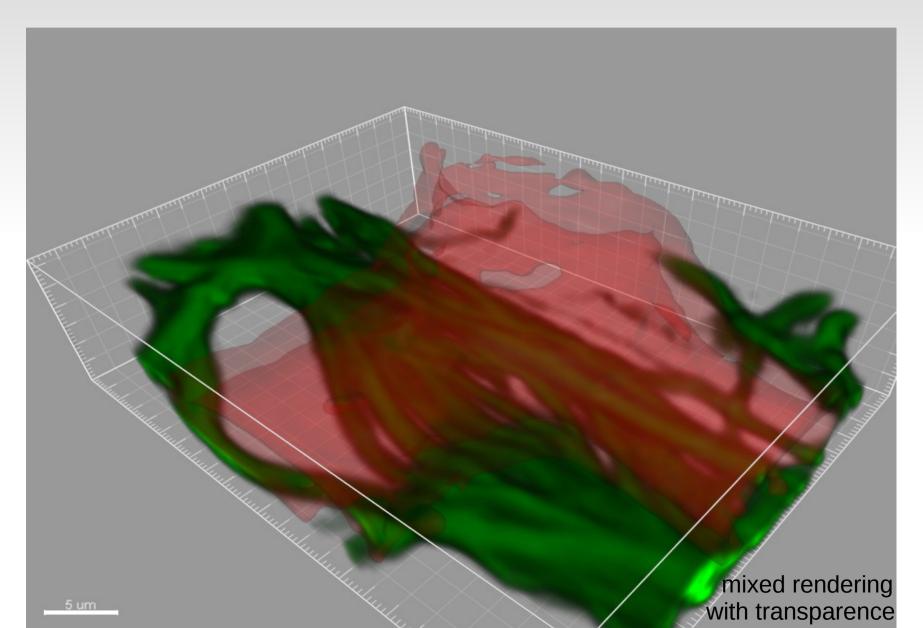
Visualization - Surface Rendering

- segmentation of the object
- surface triangulation
 - marching cubes algorithm

Visualization -Surface Rendering



Visualization - Mixed Rendering



Visualization - multi-scale data

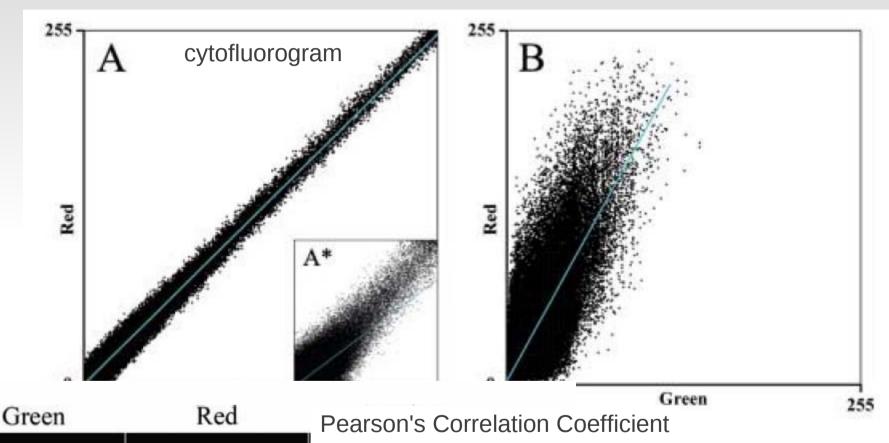
- imagine you could in one image
 - zoom smoothly from
 - organism to
 - organ to
 - tissue to
 - cells to
 - molecules
- see for example msv-project
 Multiscale Spatiotemporal Visualisation (http://www.msv-project.eu)

Colocalization Analysis

Wikipedia:

- "colocalization refers to observation of the spatial overlap between two (or more) different fluorescent labels, each having a separate emission wavelength, to see if the different "targets" are located in the same area of the cell or very near to one another."
- "correlation, ... indicative of a biological interaction"

Colocalization Analysis

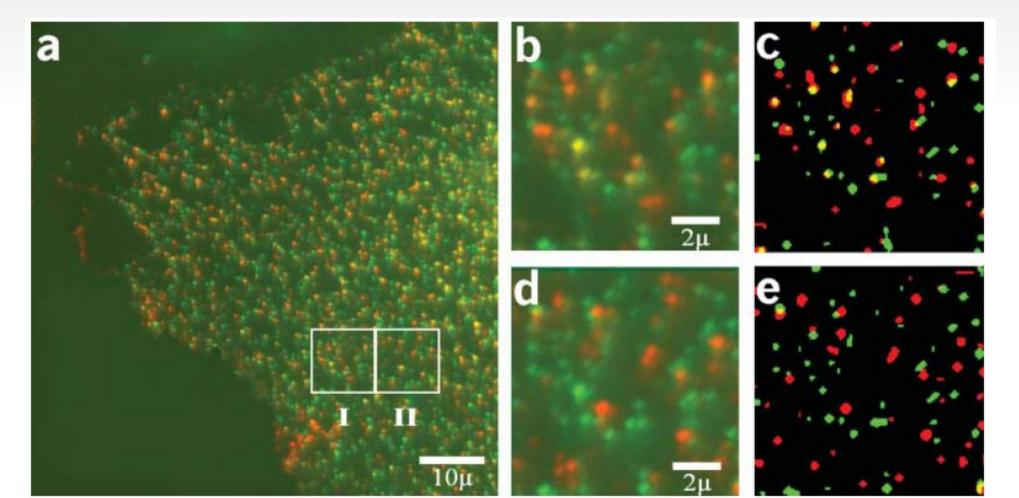


Raw ____ Duplicated

$$r_p = \frac{\sum_i (A_i - a) \times (B_i - b)}{\sqrt{\sum_i (A_i - a)^2 \times \sum_i (B_i - b)^2}}$$

Colocalization Analysis

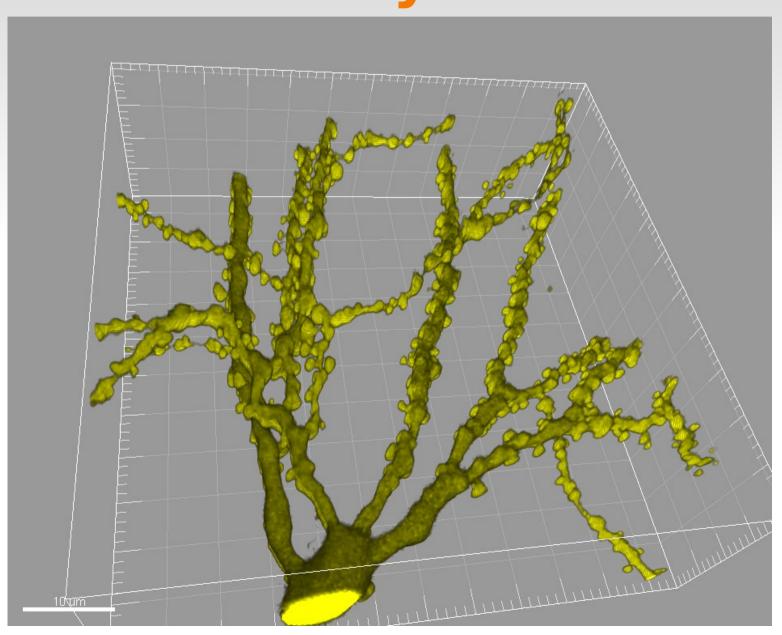
- object based colocalization
- test if distance between centroids is at resolution limit



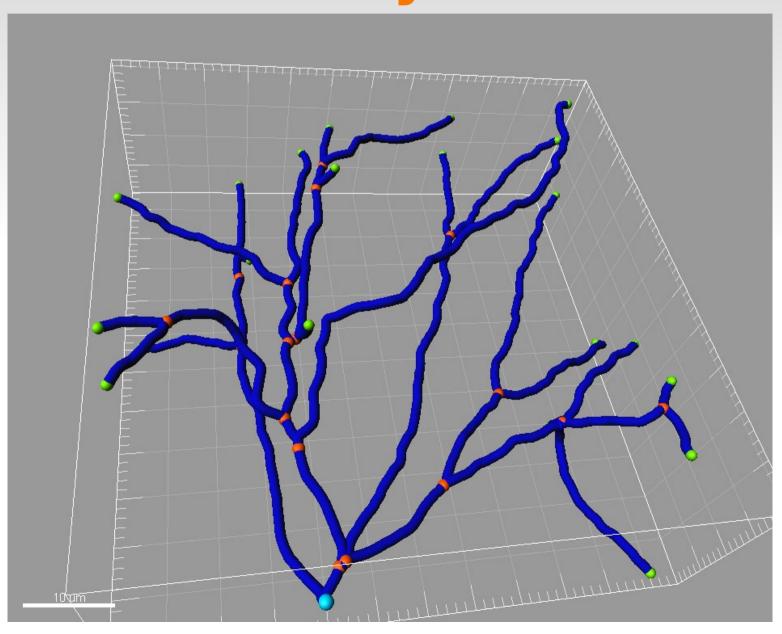
Filament tracing and analysis

- possible approach
 - second order derivatives (hessian matrix)
 - cost image
 - shortest paths
- automatic or semi-interacitve
- spine detection

Filament tracing and analysis



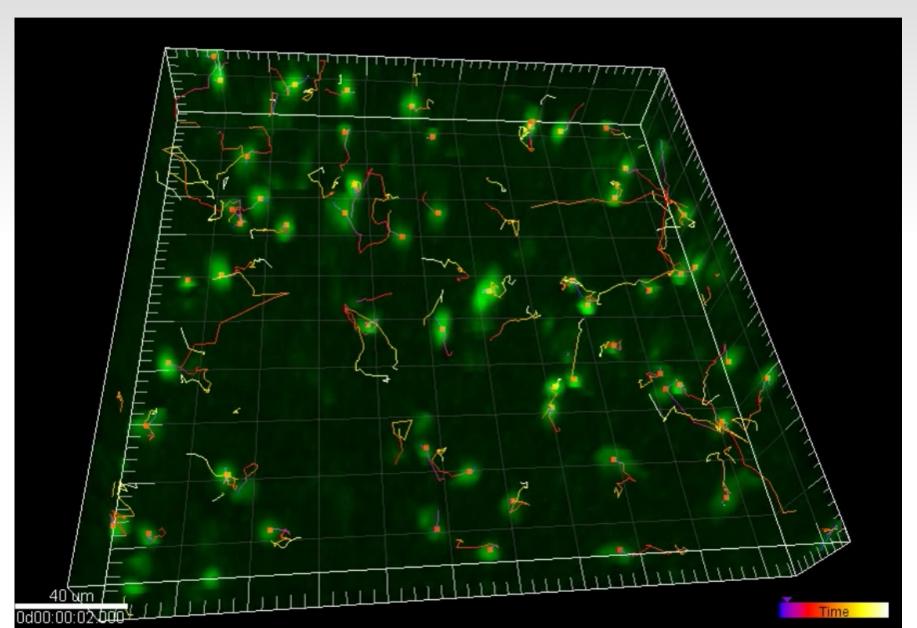
Filament tracing and analysis



Particle detection and tracking

- 2 steps
- detection of particles (spots) per time-frame
 - least-squares fitting of a gaussian mixture model to the image data
- linking of particles in successive frames
 - problem: number not constant over time

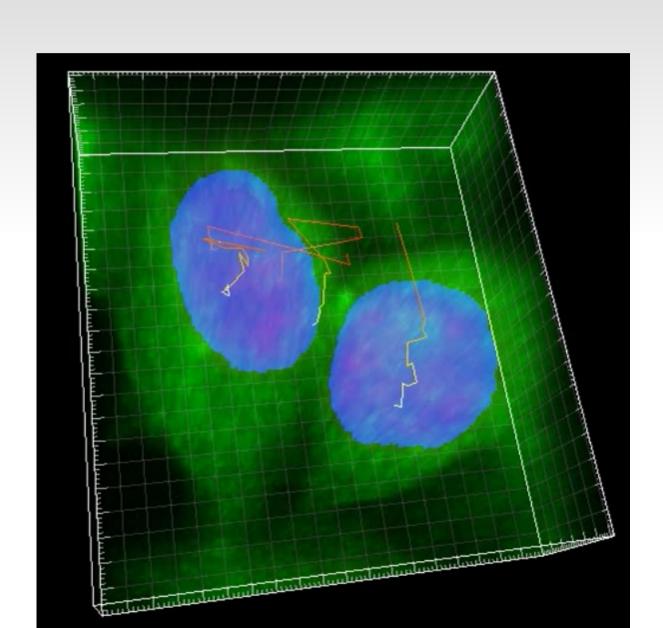
Particle detection and tracking



Cell segmentation and tracking

- cells have a distinct shape
- shape may change over time
- use active contours (snakes) to detect cells
 - active surfaces in 3D
 - shape constraint fitting to image data
- tracking
 - use contour of cell at t=n
 as initial contour for cell at t=n+1

Cell segmentation and tracking

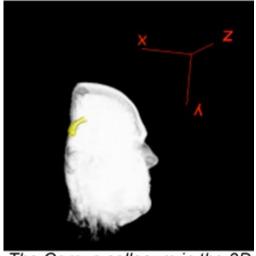


Software Tools

- Imaris (bitplane)
- Volocity (PerkinElmer)
- Avizo (vsg)
- FIJI (open source)
- ImageJ (open source)
- Matlab (MathWorks)
- huygens (svi)
 - hrm (open source)



Segmentation on a 2d slice of the Corpus callosum



The Corpus callosum in the 3D Viewer

Thank you

• Questions?







Literature

- 1.Meijering, E. & van Cappellen, **G. Biological Image Analysis Primer**. (Erasmus MC: 2006). at http://www.imagescience.org/meijering/publications/download/biap2006.pdf
- 2. Walter, T. et al. Visualization of image data from cells to organisms. Nature Methods 7, S26-S41 (2010).
- 3 R. Fisher, S. Perkins, A. Walker and E. Wolfart. **The Hypermedia Image Processing Reference** at http://homepages.inf.ed.ac.uk/rbf/HIPR2/index.htm
- 4. Baecker, V. Workshop: Image processing and analysis with ImageJ and MRI Cell Image Analyzer at http://dev.mri.cnrs.fr/wiki/imagej-workshop